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*Standards Of Fundamental Astronomy*

SOFA Astrometry Tools

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## Contents

<b>1</b>	<b>Preliminaries</b>	<b>1</b>
1.1	Introduction . . . . .	1
1.2	Quick start . . . . .	1
<b>2</b>	<b>The supported coordinate systems</b>	<b>4</b>
2.1	Catalog coordinates . . . . .	4
2.2	Current coordinates . . . . .	5
2.3	Observed coordinates . . . . .	5
<b>3</b>	<b>Design principles</b>	<b>7</b>
<b>4</b>	<b>Algorithms and accuracy</b>	<b>9</b>
4.1	Time scales . . . . .	9
4.2	Space motion and parallax . . . . .	9
4.3	Light deflection . . . . .	10
4.4	Aberration . . . . .	10
4.5	Earth attitude and rotation . . . . .	11
4.6	Terrestrial position and velocity . . . . .	11
4.7	Diurnal aberration and parallax . . . . .	11
4.8	Atmospheric refraction . . . . .	12
4.9	Overall accuracy . . . . .	12
<b>5</b>	<b>Working via a precomputed context</b>	<b>13</b>
5.1	The star-independent astrometry context . . . . .	13
5.2	Transformations using the context . . . . .	13
5.3	Using the “update time” functions . . . . .	14
<b>6</b>	<b>Example</b>	<b>15</b>
<b>7</b>	<b>Alphabetical list of functions</b>	<b>24</b>
	iauAb . . . . .	25
	iauApcg . . . . .	26
	iauApcg13 . . . . .	27
	iauApci . . . . .	28
	iauApci13 . . . . .	29
	iauApco . . . . .	30
	iauApco13 . . . . .	32
	iauApcs . . . . .	34
	iauApcs13 . . . . .	36
	iauAper . . . . .	37
	iauAper13 . . . . .	38
	iauApio . . . . .	39
	iauApio13 . . . . .	40
	iauAtci13 . . . . .	42
	iauAtciq . . . . .	43
	iauAtciqn . . . . .	44
	iauAtciqz . . . . .	46

iauAtco13 . . . . .	47
iauAtic13 . . . . .	50
iauAticq . . . . .	51
iauAtciqn . . . . .	52
iauAtio13 . . . . .	54
iauAtioq . . . . .	57
iauAtoc13 . . . . .	59
iauAtoi13 . . . . .	62
iauAtoiq . . . . .	65
iauLd . . . . .	66
iauLdn . . . . .	67
iauLdsun . . . . .	68
iauPmpx . . . . .	69
iauPvtob . . . . .	70
iauRefco . . . . .	71
<b>8 Abbreviations</b>	<b>74</b>
<b>9 References</b>	<b>75</b>
<b>Appendix</b>	<b>76</b>

# 1 Preliminaries

## 1.1 Introduction

SOFA stands for *Standards Of Fundamental Astronomy*. The SOFA software is a collection of Fortran 77 and ANSI C subprograms that implement official IAU algorithms for fundamental-astronomy computations. At the present time the SOFA software comprises 164 astronomy functions supported by 55 utility (mainly vector/matrix) functions. The core documentation for the SOFA collection consists of classified and alphabetic lists of subroutine calls plus detailed preamble comments in the source code of individual functions.

The present document looks at a selection of SOFA functions that deal with the chain of astrometric transformations linking (i) star data from a catalog and (ii) the observed direction of the incoming radiation. The scheme is shown in Figure 1 on page 2. The document provides a tutorial introduction and describes the main astrometric reference systems used by astronomers. Short examples demonstrate how to call SOFA functions to perform the sorts of transformations needed in applications that have to deal with the directions to celestial targets.

## 1.2 Quick start

Many application developers will be able to read this section of the document and ignore the rest. **Some may need only one or two functions**, namely `iauAtco13` or `iauAtci13` and/or `iauAtio13`, and these can simply be looked up in the alphabetical listing (Section 7).

Figure 1 shows the chain of transformations that link the catalog coordinates of a star to the direction in which the star is seen by an observer. The SOFA astrometry functions support all of the transformations in this chain.

Many applications will not need the whole chain. In particular it is often convenient to deal separately with the geocentric and topocentric segments, and the SOFA functions facilitate this approach. The following call performs the transformation from a star's catalog entry to its apparent coordinates at a given date, called CIRS  $[\alpha, \delta]$  in Figure 1:

---

```
iauAtci13 ( rc, dc, pr, pd, px, rv, date1, date2, &ri, &di, &eo );
```

---

`rc,dc` are the ICRS right ascension and declination at the catalog epoch, in radians; `pr,pd` are the proper motions  $(\dot{\alpha}, \dot{\delta})$  in radians per TT Julian year, `px` is the parallax in arcseconds; and `rv` is the radial velocity in km/s. `date1+date2` is the TT Julian Date. The results `ri,di` are the  $[\alpha, \delta]$  in the celestial intermediate reference system (CIRS), in radians. `eo` is the equation of the origins, and the classical geocentric apparent place is `ri-eo,di`.

The CIRS  $[\alpha, \delta]$  `ri,di` can be transformed into the observed direction, which is where a (mechanically and optically perfect) telescope would be pointed to see the star, using the following call:

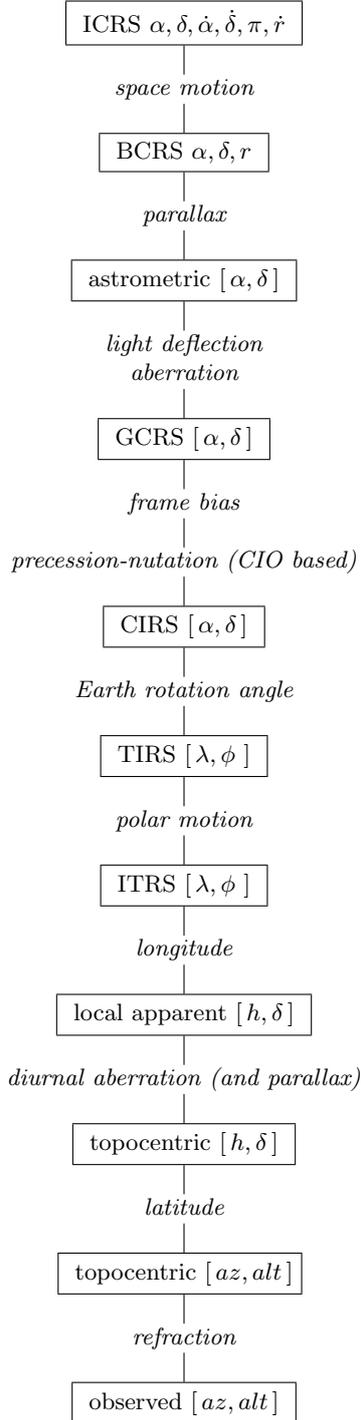


Figure 1: **The chain of astrometric transformations**

The diagram shows how the catalog entry for a star and the line of sight for a terrestrial observer are linked. For many applications, for example space observers, only a portion of the sequence is needed. Moreover, for high precision work the geocentric stage is omitted, the diurnal aberration and parallax having been subsumed into the main aberration and parallax calculations.

---

```

j = iauAtio13 ( ri, di, utc1, utc2, dut1, elong, phi, hm,
               xp, yp, phpa, tc, rh, wl,
               &aob, &zob, &hob, &dob, &rob );

```

---

`utc1+utc2` is the UTC, in a special SOFA form that is obtained by calling the `iauDtF2d` function, and `dut1` is UT1–UTC. `elong, phi` are the site longitude and geodetic latitude in radians and `hm` is the height above the WGS84 reference ellipsoid in meters. `xp, yp` are the polar motion in radians. `phpa, tc, rh` are the ambient air conditions: pressure (HPa or mB), Celsius temperature, and relative humidity (`rh=1.0` means 100%). `wl` is the effective color in  $\mu\text{m}$ ; values above 100 are treated as radio. The results `aob2, zob2, hob2, dob2, rob2` are different ways of expressing the observed direction; all are angles in radians. `aob` is azimuth, reckoned north through east; `zob` is zenith distance; `hob` is hour angle; `dob` is declination; and `rob` is right ascension (CIO based). The returned value is status, normally false. For convenience, the entire transformation from catalog to observed can be applied in a single call:

---

```

iauAtco13 ( rc, dc, pr, pd, px, rv, dx, dy, utc1, utc2, dut1,
           elong, phi, hm, xp, yp, phpa, tc, rh, wl,
           &aob2, &zob2, &hob2, &dob2, &rob2, &eo );

```

---

The three functions just introduced, namely `iauAtci13`, `iauAtio13` and `iauAtco13`, and perhaps also their inverses, `iauAtic13`, `iauAtoi13` and `iauAtoc13`, are all that will be needed by typical applications. The remainder of this document discusses more specialized aspects, including accuracy, computational efficiency, and the individual transformations in [Figure 1](#).

## 2 The supported coordinate systems

The positions of astronomical targets need to be expressed in different ways for different purposes. In the case of stars, and a terrestrial observer, three distinct needs have to be satisfied:

- A star catalog must describe the position in a way that is valid over a long period of time. The usual method is to provide the direction at a specified epoch in a coordinate system that is fixed relative to the distant background, supplemented with information about the star's space motion that allow the position to be extrapolated to any given date.
- Terrestrial observers need coordinates that are independent of location on the Earth, that are correct for the current date, and that are in a coordinate system convenient for local predictions.
- Pointing a telescope or interpreting observations requires knowledge of the ever-changing direction of the star as seen from the observing site.

The main purpose of the SOFA astrometry functions is to carry out transformations between these three types of coordinates, which we shall refer to here as *catalog*, *current* and *observed*, respectively. For space observers, only a portion of the chain is relevant, from ICRS to the Geocentric Celestial Reference System (GCRS). Other applications, such as groundbased interferometers, may stop at topocentric coordinates, omitting refraction.

### 2.1 Catalog coordinates

A star catalog can be constructed using any coordinate system that is fixed relative to the cosmological background: the choices of pole and longitude zero-point are essentially arbitrary. For some purposes galactic coordinates are convenient, while for some classical applications ecliptic coordinates are a natural choice, based on the mean (*i.e.* precessing) ecliptic pole and equinox at some particular epoch. Most historical star catalogs have used a reference system based on the mean pole and equinox for a specified standard epoch such as B1950.0 or J2000.0. The choice is convenient for casual use as the tabulated mean right ascensions and declinations are sufficiently close to current  $[\alpha, \delta]$  for rough (within a degree or two) predictions of observed direction without the bother of applying precession corrections.

The SOFA astrometry functions support just one catalog system, namely the International Celestial Reference System (ICRS). This can be seen as the start of the chain shown in Figure 1.

When the ICRS was set up, a completely arbitrary orientation of the coordinate axes could have been chosen. However, to ease the transition, the new system was nominally oriented to match J2000.0 mean  $[\alpha, \delta]$ : the accuracy achieved was of order 25 milliarcseconds (mas). The two systems are sufficiently close that for many everyday applications the distinction between the two can be ignored. However, for precise applications, such as interferometry, other SOFA functions provide high-accuracy transformations between mean J2000.0  $[\alpha, \delta]$  (and also the FK5 realization) and ICRS.

Where ICRS coordinates are the end point rather than the starting point, they are referred to as “astrometric”. Such positions clearly have no space motion or parallax information and are indistinguishable from the coordinates of a cosmological source lying in the same apparent direction on the date in question.<sup>1</sup>

## 2.2 Current coordinates

The “current” coordinates are the intermediary stage between a star’s catalog entry and the direction seen by the observer. The SOFA astrometry functions use the Celestial Intermediate Reference System (CIRS) for this purpose. The pole is the celestial intermediate pole (CIP), and the  $\alpha$  zero-point the kinematically-defined celestial intermediate origin (CIO). In this system, hour angle  $h$  is related to right ascension through the local Earth rotation angle:  $h = \theta - \alpha$ , where  $\theta$  is ERA +  $\lambda$  and  $\lambda$  is longitude (east positive).

The classical system, also supported by the SOFA functions but in an ancillary capacity, is geocentric apparent place. This has the same pole as CIRS, namely the CIO, and hence declinations in the two systems are the same. However, the  $\alpha$  zero-point in this case is the equinox, which is defined geometrically as the ascending node of the ecliptic of date on the CIO equator. The formula linking  $h$  and  $\alpha$  is the same as for CIRS, namely  $h = \theta - \alpha$ , except that now  $\theta$  is the local apparent sidereal time.

Both the classical and CIRS methods yield identical hour angles. But the advantage of CIRS is that precession-nutation affects only the orientation of the Earth’s axis: the  $\alpha$  zero-point is an entirely separate matter. In the classical approach, the  $\alpha$  zero-point undergoes a complicated and comparatively rapid motion, only to be cancelled out by the inclusion in the Greenwich apparent sidereal time (GST) formula of a complicated set of polynomial and Poisson terms. The CIRS  $\alpha$  zero-point is almost stationary<sup>2</sup> and the Earth rotation measure, in this case ERA, is just a linear transformation of universal time UT1. The bridge between the classical and CIRS systems is the *equation of the origins*, which is ERA – GST or equivalently  $\alpha_{\text{CIRS}} - \alpha_{\text{apparent}}$ ; its value is returned by several of the SOFA astrometry functions in case it is needed.

## 2.3 Observed coordinates

The “observed” [ $az, alt$ ] means the direction in which a mechanically and optically perfect theodolite<sup>3</sup> would be pointed in order to see the target. This is the natural coordinate system in which to express the observed position as it differs from the topocentric, *i.e.* unrefracted, position only by a change in altitude. However, it is just as valid to apply the standard altaz-to-equatorial transformation and so obtain observed [ $h, \delta$ ], and then to combine this with an Earth rotation measure to yield an observed [ $\alpha, \delta$ ]. In the [ $h, \delta$ ] and [ $\alpha, \delta$ ] cases the direction

<sup>1</sup>The SOFA astrometry functions implement astrometric place quite literally, and when transforming them to current coordinates includes light deflection as well as stellar aberration. Applications that deal with targets in the inner solar system will need to cope with the case of transits across the Sun, where very large spurious deflections will occur, corresponding to sources lying *behind* the Sun.

<sup>2</sup>Throughout the 20<sup>th</sup> and 21<sup>st</sup> centuries the CIO remains within 0".1 of the ICRS meridian.

<sup>3</sup>aligned to ITRS north and the geodetic vertical

is as seen by a mechanically and optical perfect equatorial telescope, with its polar axis aligned to the CIP.

The SOFA astrometry functions support all of these different options. However, instead of altitude, zenith distance is returned. The main reason for this is to remove any ambiguity over which horizon (apparent, astronomical, geometric *etc.*) is being used, making it clear that such distinctions are the responsibility of the application. Another reason is to sidestep the interchangeable use of “altitude” and “elevation”: the former is considered more correct but the latter is more common, especially in radio astronomy.

### 3 Design principles

The SOFA astrometry functions design principles are these:

1. The transformations that are most commonly needed should be achievable in a single call.
2. Where practical, the highest standards of accuracy should be available...
3. ... but this must not be at the expense of ease of use.
4. Computational efficiency matters but should not complicate applications where this aspect is unimportant.

The ways these needs are addressed are as follows:

1. The transformations catalog to current, current to observed, and catalog to observed, plus inverses, are each implemented as a single function.
2. There are two sets of functions. One set uses the latest SOFA models; the other accepts values (for example Earth ephemerides or refraction constants) that the user supplies.
3. Rigorous algorithms, consistent with special and general relativity, are used. However, aspects that only a specialist would need and that would complicate the programming interfaces unacceptably (for example requiring detailed solar system ephemerides or weather information) are not provided for. Even then, the interfaces are flexible enough to allow expert users to overcome these limitations.
4. To achieve computational efficiency, the problem is separated into two components: (i) populating a context containing star-independent parameters and (ii) using the precomputed context to carry out a specific transformation quickly. Thus in a case where the same transformation is to be applied to many different stars, (i) is carried out just once and (ii) is applied to the stars one by one. In a case where efficiency is not important, a single function is called that simply performs (i) followed by (ii).

The single-call transformations using standard SOFA models are the following:

<code>iauAtci13</code>	ICRS to CIRS, 2013 models
<code>iauAtco13</code>	ICRS to observed, 2013 models
<code>iauAtic13</code>	CIRS to ICRS astrometric, 2013 models
<code>iauAtio13</code>	CIRS to observed, 2013 models
<code>iauAtoc13</code>	observed to ICRS astrometric, 2013 models
<code>iauAtoi13</code>	observed to CIRS, 2013 models

There are no counterparts for the case where the user wishes to substitute his own models. Instead he simply sets up the context himself before calling the appropriate “quick” transformation.

To populate the context using standard SOFA models, a range of functions is provided. The choice depends on the observer (terrestrial, geocentric, space) and which segment of the transformation chain is required:

<code>iauApcg13</code>	astrometry parameters, ICRS-GCRS, geocenter, 2013 models
<code>iauApci13</code>	astrometry parameters, ICRS-CIRS, 2013 models
<code>iauApc13</code>	astrometry parameters, ICRS-observed, 2013 models
<code>iauApcs13</code>	astrometry parameters, ICRS-GCRS, space observer, 2013 models
<code>iauApio13</code>	astrometry parameters, CIRS-observed, 2013 models

In addition, there is a function that updates only the Earth rotation angle. This is useful in applications such as telescope control, where it is acceptable to update the catalog to current transformation less frequently than the Earth rotation:

<code>iauAper13</code>	astrometry parameters: update ERA, 2013
------------------------	---

There is a full set of counterparts that accept models supplied by the user:

<code>iauApcg</code>	astrometry parameters, ICRS-GCRS, geocenter
<code>iauApci</code>	astrometry parameters, ICRS-CIRS
<code>iauApc13</code>	astrometry parameters, ICRS-observed
<code>iauApcs</code>	astrometry parameters, ICRS-GCRS, space observer
<code>iauApio</code>	astrometry parameters, CIRS-observed

and:

<code>iauAper</code>	astrometry parameters: update ERA
----------------------	-----------------------------------

The above are all the functions that populate the context. The functions that use the context to perform an individual transformation are as follows:

<code>iauAtciq</code>	quick ICRS to CIRS
<code>iauAtciqn</code>	quick ICRS to CIRS, multipel deflections
<code>iauAtciqz</code>	quick astrometric ICRS to CIRS
<code>iauAticq</code>	quick CIRS to ICRS astrometric
<code>iauAticqn</code>	quick CIRS to ICRS astrometric, multiple deflections
<code>iauAtioq</code>	quick CIRS to observed
<code>iauAtoiq</code>	quick observed to CIRS

The remaining functions, less likely to be called directly by applications, are as follows:

<code>iauAb</code>	stellar aberration
<code>iauLd</code>	light deflection by a single solar-system body
<code>iauLdn</code>	light deflection by multiple solar-system bodies
<code>iauLdsun</code>	light deflection by the Sun
<code>iauPmpx</code>	proper motion and parallax
<code>iauPvtob</code>	position/velocity of terrestrial station
<code>iauRefco</code>	refraction constants for given ambient conditions

## 4 Algorithms and accuracy

The SOFA astrometry functions use modern and rigorous models as far as possible, and are capable of reaching microrcosecond accuracy in favourable cases. The one major exception is atmospheric refraction, for which definitive models do not exist.

Notes on some of the transformation steps shown in Figure 1 follow; for references see Page 75. For a definitive description of the algorithms is the source code itself should be consulted.

### 4.1 Time scales

The different SOFA astrometry functions require times to be expressed in the appropriate time scale, which can be TDB, UTC or in one case UT1.

Although many of the functions ask for barycentric dynamical time, TDB, it is always acceptable to use instead the more accessible terrestrial time, TT. The difference is always less than 2 ms, wholly negligible for computing aberration and precession for the types of application under consideration here. TDB is complicated and expensive to compute (see `iauDtDb`) and the recommendation is simply to use TT instead.

However, the distinction between UTC and TT/TDB, currently over a minute, *is* significant, at least for applications that require milliarcsecond precision or better.

Where observed place is concerned, universal time must of course be used, and this means knowing not just UTC but the current UT1–UTC, which is available from IERS bulletins. In the case of `iauAper13`, UT1 itself is required rather than UTC.

### 4.2 Space motion and parallax

Starting with the star’s catalog data, the function `iauPmpx` computes its *coordinate direction* by allowing for proper motion and parallax.

A conventional non-relativistic proper motion is used, which assumes constant speed through space. The algorithm is an adaptation of Eq. (7.24) in Urban & Seidelmann (2013). For a star with non-zero radial velocity, there is a foreshortening effect caused by the changing light time, so that the star’s path is not as given by the conventional algorithm. However, once the changing light time is applied to the extrapolation interval, the effect cancels out. Consequently, the simple algorithm in fact delivers the correct result.

The algorithm is conveniently tolerant of physically impossible star data, in particular combinations of small parallax and finite proper motion that imply superluminal speed. It also agrees to microarcsecond accuracy with a fully relativistic treatment. However, should an application prefer the latter, suitable code is provided in Appendix A.

One departure from normal practice is that the proper motion calculation includes a first-order correction for the *Rømer effect*. This is the small modulation (annual for terrestrial observers) of the proper motion caused by the changing light time. The effect exceeds 100  $\mu$ as only in the case of Barnard’s Star.

### 4.3 Light deflection

The deflection of the light from the target as it passes through the gravitational field of a solar-system body is calculated by the function `iauLd`. Applying the total of all such deflections to the coordinate direction yields *natural direction*. For typical applications only the Sun (at most) need be considered, and, for convenience, a separate function is provided for that purpose: `iauLdsun`. A further function, `iauLdn`, provides a deflection calculation for multiple solar-system bodies, for example Sun + Jupiter + Saturn.

The function `iauLd` is quite general. The algorithm is based on Eq. (70) in Klioner (2003) and Eq. (7.63) in Urban & Seidelmann (2013), with some rearrangement to minimize the impact of machine precision. Its arguments include (among other things) the mass of the body and full details of the geometrical arrangement. The latter means the function is valid for solar-system targets as well as distant objects, which is not strictly true for either `iauLdsun` or `iauLdn`.

The precise calculation of light deflection close to a solar-system body is complicated, and the SOFA functions do not attempt the complete treatment set out in Klioner (2003). However, effects such as quadrupole field can be allowed for by making an *ad hoc* adjustment to the mass argument, based on the relative disposition of the body and the light ray.

In an advanced application where multiple gravitating bodies are being included, the function `iauLd` can be called for each body in succession (in the order in which the light passed the different bodies on its way to the observer, though this is not critical). Alternatively, for stars and other distant targets the `iauLdn` function can be called, with the data for the successive bodies supplied in an array. The calculation relies on accurate ephemerides, at least when the target and deflecting body are close together in the sky, and the application needs access to a suitable solar-system ephemeris such as DE405.

The algorithm used by `iauLd` is merely an analytical approximation: a rigorous treatment would involve numerical integration along the path of the light-ray and is impractical. Consequently, a question arises concerning what time to use when interrogating the body's ephemeris. A convenient option that gives good results is to use the time at which the light passed closest to the body, and this is what `iauLdn` does, using the body's barycentric velocity at the time of observation to back-track its position by the time since the light passed by (but only if the source lies behind the body). In the case of `iauLdsun`, this step is omitted, in accordance with convention. This is justifiable because the Sun's barycentric velocity is small and because in grazing cases other approximations dominate (at the 0.5 mas level). However, if `iauLdn` used, the Sun is treated in the same way as the planets, and so the light-time correction *is* applied, making at most a 0.1 mas difference compared with the `iauLdsun` result.

### 4.4 Aberration

Stellar aberration can be applied to the natural direction using the `iauAb` function. The result is called the *proper direction* and is the direction in which the radiation is seen. The algorithm is based on Eq. (7.40) in Urban & Seidelmann (2013), but with two improvements. First, rigorous rather than approximate normalization is applied at the end; second, the  $0.4 \mu\text{as}$  gravitational potential term from Eq. (7) in Klioner (2003) is added, evaluated for the Sun alone. The

algorithm is capable of sub-microarcsecond accuracy. However, the limitation in practice is likely to be the accuracy of the supplied Earth (or observer) velocity. For example, if the SOFA `iauEpv00` function is used, errors of up to  $5 \mu\text{as}$  can occur.

If the velocity of the geocenter is specified, the call to `iauAb` computes the conventional annual aberration, to which diurnal aberration will later be added as part of the topocentric calculation. If instead the observer's velocity is specified, the entire aberration is computed in one go and no diurnal aberration will be needed. The latter approach is in fact more rigorous and avoids spurious cross terms that can exceed  $30 \mu\text{as}$ . (Another  $30 \mu\text{as}$  effect that is conventionally neglected is diurnal parallax, and this can also be avoided by working directly to the observer rather than using geocentric coordinates as an intermediate stage.)

#### 4.5 Earth attitude and rotation

The orientation of the CIRS in the GCRS requires knowledge of both the pole coordinates and the location of the  $\alpha$  zero-point. The pole is the CIO, and its position includes the offset at J2000.0, called *frame bias*, the accumulated precession from that epoch to date, and the current nutation. The SOFA astrometry functions use the CIO as the  $\alpha$  zero-point. In the completely general SOFA astrometry functions such as `iauApco`, the orientation is specified as the CIO coordinates  $(X, Y)$  and the value of the CIO locator  $s$ . Rigorous vector methods are used throughout.

In the functions that for convenience use current SOFA models, such as `iauApco13`, the bias and precession come from IAU 2006 models and the nutation is IAU 2000A. The IAU 2006/2000A models are (at present) accurate to 1 mas, limited by the unmodeled free core nutation, an accuracy that is adequate for most applications. Applications that require the utmost accuracy should instead call `iauApco` *etc.* and supply CIP  $(X, Y)$  using data published by the International Earth Rotation and Reference systems Service (IERS).

#### 4.6 Terrestrial position and velocity

The position and velocity of the terrestrial observer in the CIRS are calculated using the `iauPvtob` function. This is called even by the general functions, not just those using SOFA models, as the effects of small differences such as choice of reference ellipsoid are always too small to matter: `iauPvtob` assumes the WGS84 ellipsoid and the Earth rotation rate from the IAU 2000 ERA formula. However, the use of the `iauSp00` function to compute the TIO locator  $s'$  is reserved for the SOFA-model functions. Polar motion is taken into account, and along with  $s'$  is applied using rigorous vector methods.

#### 4.7 Diurnal aberration and parallax

Where the user has elected to break the chain at the CIRS stage, diurnal aberration is applied separately using a simple first-order vector expression and diurnal parallax is neglected. The end-to-end ICRS  $\leftrightarrow$  observed transformations eliminate the intermediate step, adding the observer's position and velocity to the Earth's and eliminating these compromises.

## 4.8 Atmospheric refraction

As mentioned earlier, no definitive models for atmospheric refraction exist. The available models differ in accuracy, computational overheads, wavelength coverage, performance in different zenith-distance ranges and convenience of use. The simple model used by SOFA in the functions `iauRefco`, `iauAtioq` and `iauAtoiq` is concise, fast and more than accurate enough for most practical applications. However, more-demanding users have the option to substitute something better suited to their particular needs.

The SOFA model uses the familiar  $A \tan \zeta + B \tan^3 \zeta$  formula, but with special measures to improve the results near the horizon. The constants  $A$  and  $B$  are obtained by calling `iauRefco`; the arguments are the pressure, temperature and relative humidity at the observer, plus the observing wavelength. Sufficiently long wavelengths (greater than 0.1 mm) are interpreted as radio.

In tests over a wide range of trial conditions, and down to  $\zeta = 75^\circ$ , the accuracy of the algorithm was compared with a more rigorous raytracing method. In the optical/IR the results were better than 10 mas RMS and about 60 mas worst case, while in the radio the figures were better than 50 mas RMS and about 300 mas worst case.

For more on the refraction-constant algorithm and detailed test results, see the `iauRefco` description on Page 71.

## 4.9 Overall accuracy

The accuracy delivered by the SOFA functions depends on circumstances:

- All transformations that involve observed place are limited by the refraction predictions. This is likely to be true even if better refraction constants are supplied than those from the very basic model used by `iauRefco`. Even the best available refraction models probably in practice struggle to achieve  $0''.1 \tan \zeta$ .
- For transformations not involving refraction, the IAU 2000A/2006 precession-nutation model limits the accuracy to about 1 mas at the time of writing.
- Over much of the sky, SOFA's predictions of light deflection by the Sun are accurate to  $1 \mu\text{as}$ . Close to the Sun the errors may approach the 0.5 mas level. Close to other solar-system bodies, unmodeled deflections of several milliarcseconds can arise, for example over 16 mas at Jupiter's limb. This can be avoided by using the functions `iauAtciqn`, `iauAicqn` and `iauLdn`.
- If the `iauEpv00` function is used for the Earth ephemeris, errors in the aberration predictions of up to  $5 \mu\text{as}$  can occur. Note that an error in the observer's speed of 1.5 mm/s gives an aberration error of about  $1 \mu\text{as}$ .

Care is taken to ensure that given transformations and their inverses match to high precision. Where this is not achievable simply through rigor (by the use of vector methods for example) iteration is used. Without refraction, the inversions are self-consistent to better than  $1 \mu\text{as}$  all over the celestial sphere. With refraction included, consistency falls off at high zenith distances, but is still better than  $0''.05$  at  $\zeta = 85^\circ$ .

## 5 Working via a precomputed context

The SOFA astrometry functions operate in two stages:

- First a set of star-independent parameters is set up;
- then this pre-computed context is used to perform the required transformations for a particular target.

Internally, this is how the convenient one-call functions work, but the technique can also be used at the application level. The usual reason to do so is that there is a large number of targets to be transformed and the overheads of repeating onerous computations (such as evaluation of lengthy nutation series) are best avoided. However, another advantage of the scheme is flexibility, giving access to more transformation options than the pre-packaged single calls cover. An example is where the user has access to more accurate data (Earth ephemeris, precession-nutation, refraction) than is available merely by evaluating standard SOFA models.

### 5.1 The star-independent astrometry context

The context, which is a `struct` of type `iauASTROM`, provides for the whole chain of astrometric transformations  $\text{ICRS} \leftrightarrow \text{GCRS} \leftrightarrow \text{CIRS} \leftrightarrow \text{observed}$ . However, it is not necessary to populate the context in full when only a partial transformation is needed. The location of the observer also affects how much of the content is needed. The following table shows all of the various options:

<i>functions</i>		<i>observer</i>	<i>transformation</i>
<code>iauApio</code>	<code>iauApio13</code>	terrestrial	CIRS $\leftrightarrow$ observed
<code>iauApci</code>	<code>iauApci13</code>	terrestrial	ICRS $\leftrightarrow$ CIRS
<code>iauApcg</code>	<code>iauApcg13</code>	geocentric	ICRS $\leftrightarrow$ GCRS
<code>iauApcs</code>	<code>iauApcs13</code>	space	ICRS $\leftrightarrow$ GCRS
<code>iauApco</code>	<code>iauApco13</code>	terrestrial	ICRS $\leftrightarrow$ observed
<code>iauAper</code>	<code>iauAper13</code>	terrestrial	update Earth rotation alone

As set out in Figure 1, the transformation from ICRS to GCRS covers space motion, parallax, light deflection, and aberration; that from GCRS to CIRS comprises frame bias and precession-nutation; that from CIRS to observed takes account of Earth rotation, polar motion, diurnal aberration and parallax (unless subsumed into the ICRS  $\leftrightarrow$  GCRS transformation), and atmospheric refraction. Those functions with names ending in “13” use contemporary SOFA models to compute the various ephemerides. The others accept ephemerides supplied by the caller.

### 5.2 Transformations using the context

After populating the context, the transformation for each target is carried out as follows:

<i>transformation</i>	<i>call(s)</i>
ICRS → GCRS	<code>iauAtciq*</code>
ICRS → CIRS	<code>iauAtciq*</code>
ICRS → observed	<code>iauAtciq* then iauAtioq</code>
GCRS → ICRS	<code>iauAticq</code>
CIRS → ICRS	<code>iauAtciq</code>
CIRS → observed	<code>iauAtioq</code>
observed → ICRS	<code>iauAtoiq then iauAticq*</code>
observed → CIRS	<code>iauAtoiq</code>

Transformations not shown are unlikely to be needed and/or can be carried out using other SOFA functions, for example those that deal with precession-nutation.

The internals of the context structure are defined in the header file `sofam.h`. However, applications should not make direct use of this information, in case the design changes in the future.

### 5.3 Using the “update time” functions

The functions `iauAper` and `iauAper13` update only part of the context structure, namely the Earth rotation angle. In groundbased applications such as telescope control systems, this allows the efficient generation of a stream of positions as time progresses. It is not rigorous, because everything is moving, but the Earth rotation is by far the fastest effect, at about  $15^\circ$  per hour.

The rate at which the other contributions are changing are several orders of magnitude less: the maximum hourly changes in diurnal aberration, annual aberration and precession are about 80 mas, 15 mas and 6 mas respectively, which is negligible. It is therefore commonplace to perform the ICRS → CIRS transformation (or the classical equivalent, mean → apparent) just once, for target acquisition, and to leave it fixed for subsequent tracking. Even advanced control systems for large telescopes rarely bother to recompute the full transformation more often than once a minute or so.

## 6 Example

Starting with catalog data for a star, the demonstration program listed below performs a whole series of transformations, namely:

1. ICRS to CIRS.
2. The reverse, giving the astrometric place.
3. Astrometric place to CIRS.
4. Geocentric apparent place *via* the equation of the origins.
5. CIRS to topocentric, *i.e.* CIRS to observed but with zero air pressure.
6. CIRS to observed.
7. ICRS to observed in a single call.
8. ICRS to CIRS using JPL DE405 for the Earth ephemeris.
9. The same but including light deflection by Jupiter and Saturn.
10. The reverse, to check agreement with Step 2.

The code is complete, ready to compile and run, and may be a useful template for further experiments. A real-life application would of course be far simpler than this quite complicated demonstration, with the use of SOFA astrometry functions limited to perhaps a single call.

The test circumstances are as follows. It must be stressed that all the numbers have been adopted purely for the sake of the demonstration and have no other significance. Although quite representative of real data, **all of the values used must be assumed to be fictitious.**

The site coordinates are:

Latitude and longitude = S 30° 14' 26".731 W 70° 44' 11".560

Height above the reference ellipsoid = 2738m

Here are the catalog data for the test star:

ICRS  $[\alpha, \delta] = 14^{\text{h}} 34^{\text{m}} 16^{\text{s}}.81183 -12^{\circ} 31' 10''.3965$

proper motions:  $\mu_{\alpha} = -354.45 \text{ mas/y}$ ,  $\mu_{\delta} = +595.35 \text{ mas/y}$

parallax = 0".16499

radial velocity (recession speed) = 0 km/s

The date and time are:

2013 April 2, 23<sup>h</sup> 15<sup>m</sup> 43<sup>s</sup>.55 UTC

The Earth orientation parameters are:

polar motion:  $x = +50.995$  mas,  $y = +376.723$  mas

UT1–UTC = +155.0675 ms

and also:

corrections to IAU 2000A CIP:  $dx = +0.269$  mas,  $dy = -0.274$  mas

The demonstration code follows.

---

```
#include <sofa.h>
void reprd ( char*, double, double );
int main ()
{
    iauASTROM astrom;
    iauLDBODY b[3];
    double phi, elong, hm, phpa, tc, rh, wl, utc1, utc2, tai1, tai2,
           tt1, tt2, xp, yp, dut1, dx, dy, rc, dc, pr, pd, px, rv,
           eo, ri, di, rca, dca, ra, da, aot, zot, hot, dot, rot,
           aob, zob, hob, dob, rob,
           pvh[2][3], pvb[2][3], r[3][3], x, y, s;

    /* Site longitude, latitude (radians) and height above the geoid (m). */
    iauAf2a ( '-', 70, 44, 11.560, &phi );
    iauAf2a ( '-', 30, 14, 26.731, &elong );
    hm = 2738.0;

    /* Ambient pressure (hPa), temperature (C) and rel. humidity (frac). */
    phpa = 731.0;
    tc = 12.8;
    rh = 0.59;

    /* Effective color (microns). */
    wl = 0.55;

    /* UTC date. */
    if ( iauDtf2d ( "UTC", 2013, 4, 2, 23, 15, 43.55,
                  &utc1, &utc2 ) ) return -1;

    /* TT date. */
    if ( iauUtctai ( utc1, utc2, &tai1, &tai2 ) ) return -1;
    if ( iauTaitt ( tai1, tai2, &tt1, &tt2 ) ) return -1;

    /* EOPs: polar motion in radians, UT1-UTC in seconds. */
    xp = 50.995e-3 * DAS2R;
    yp = 376.723e-3 * DAS2R;
    dut1 = 155.0675e-3;

    /* Corrections to IAU 2000A CIP (radians). */
    dx = 0.269e-3 * DAS2R;
    dy = -0.274e-3 * DAS2R;

    /* Star ICRS RA,Dec (radians). */
    if ( iauTf2a ( ' ', 14, 34, 16.81183, &rc ) ) return -1;
    if ( iauAf2a ( '-', 12, 31, 10.3965, &dc ) ) return -1;
```

```

reprd ( "ICRS, epoch J2000.0:", rc, dc );

/* Proper motion: RA/Dec derivatives, epoch J2000.0. */
pr = atan2 ( -354.45e-3 * DAS2R, cos(dc) );
pd = 595.35e-3 * DAS2R;

/* Parallax (arcsec) and recession speed (km/s). */
px = 164.99e-3;
rv = 0.0;

/* ICRS to CIRS (geocentric observer). */
iauAtci13 ( rc, dc, pr, pd, px, rv, tt1, tt2, &ri, &di, &eo );
reprd ( "catalog -> CIRS:", ri, di );

/* CIRS to ICRS (astrometric). */
iauAtic13 ( ri, di, tt1, tt2, &rca, &dca, &eo );
reprd ( "CIRS -> astrometric:", rca, dca );

/* ICRS (astrometric) to CIRS (geocentric observer). */
iauAtci13 ( rca, dca, 0.0, 0.0, 0.0, 0.0, tt1, tt2, &ri, &di, &eo );
reprd ( "astrometric -> CIRS:", ri, di );

/* Apparent place. */
ra = iauAnp ( ri - eo );
da = di;
reprd ( "geocentric apparent:", ra, da );

/* CIRS to topocentric. */
if ( iauAtio13 ( ri, di, utc1, utc2, dut1, elong, phi, hm, xp, yp,
                0.0, 0.0, 0.0, 0.0,
                &aot, &zot, &hot, &dot, &rot ) ) return -1;
reprd ( "CIRS -> topocentric:", rot, dot );

/* CIRS to topocentric. */
if ( iauAtio13 ( ri, di, utc1, utc2, dut1, elong, phi, hm, xp, yp,
                phpa, tc, rh, wl,
                &aob, &zob, &hob, &dob, &rob ) ) return -1;
reprd ( "CIRS -> observed:", rob, dob );

/* ICRS to observed. */
if ( iauAtco13 ( rc, dc, pr, pd, px, rv, utc1, utc2, dut1,
                elong, phi, hm, xp, yp, phpa, tc, rh, wl,
                &aob, &zob, &hob, &dob, &rob, &eo ) ) return -1;
reprd ( "ICRS -> observed:", rob, dob );

/* ICRS to CIRS using some user-supplied parameters. */

/* SOFA heliocentric Earth ephemeris. */

```

```

    if ( iauEpv00 ( tt1, tt2, pvh, pvb ) ) return -1;

/* JPL DE405 barycentric Earth ephemeris. */
pvb[0][0] = -0.9741704366519668;
pvb[0][1] = -0.2115201000882231;
pvb[0][2] = -0.0917583114068277;
pvb[1][0] =  0.0036436589347388;
pvb[1][1] = -0.0154287318503146;
pvb[1][2] = -0.0066892203821059;

/* IAU 2000A CIP. */
iauPnm00a ( tt1, tt2, r );
iauBpn2xy ( r, &x, &y );

/* Apply IERS corrections. */
x += dx;
y += dy;

/* SOFA CIO locator. */
s = iauS06 ( tt1, tt2, x, y );

/* Populate the context. */
iauApci ( tt1, tt2, pvb, pvh[0], x, y, s, &astrom );

/* Carry out the transformation and report the results. */
iauAtciq ( rc, dc, pr, pd, px, rv, &astrom, &ri, &di );
reprd ( "ICRS -> CIRS (JPL, IERS):", ri, di );

/* The same but with Saturn then Jupiter then Sun light deflection. */

b[0].bm = 0.00028574;
b[0].dl = 3e-10;
b[0].pv[0][0] = -7.8101442680818964;
b[0].pv[0][1] = -5.6095668114887358;
b[0].pv[0][2] = -1.9807981923749924;
b[0].pv[1][0] =  0.0030723248971152;
b[0].pv[1][1] = -0.0040699547707598;
b[0].pv[1][2] = -0.0018133584165345;

b[1].bm = 0.00095435;
b[1].dl = 3e-9;
b[1].pv[0][0] =  0.7380987962351833;
b[1].pv[0][1] =  4.6365869247538951;
b[1].pv[0][2] =  1.9693136030111202;
b[1].pv[1][0] = -0.0075581692172088;
b[1].pv[1][1] =  0.0012691372216750;
b[1].pv[1][2] =  0.0007279990012801;

```

```

b[2].bm = 1.0;
b[2].dl = 6e-6;
b[2].pv[0][0] = -0.0007121743770509;
b[2].pv[0][1] = -0.0023047830339257;
b[2].pv[0][2] = -0.0010586596574639;
b[2].pv[1][0] = 0.0000062923521264;
b[2].pv[1][1] = -0.0000003308883872;
b[2].pv[1][2] = -0.0000002964866231;

iauAtciqn ( rc, dc, pr, pd, px, rv, &astrom, 3, b, &ri, &di );
reprd ( "ICRS -> CIRS (+ planets):", ri, di );

/* CIRS to ICRS (astrometric). */
iauAticqn ( ri, di, &astrom, 3, b, &rca, &dca );
reprd ( "CIRS -> astrometric:", rca, dca );

return 0;
}
#include <stdio.h>
void reprd ( char* s, double ra, double dc )
{
    char pm;
    int i[4];

    printf ( "%25s", s );
    iauA2tf ( 7, ra, &pm, i );
    printf ( " %2.2d %2.2d %2.2d.%7.7d", i[0],i[1],i[2],i[3] );
    iauA2af ( 6, dc, &pm, i );
    printf ( " %c%2.2d %2.2d %2.2d.%6.6d\n", pm, i[0],i[1],i[2],i[3] );
}

```

The program produces the following report:

---

```

ICRS, epoch J2000.0: 14 34 16.8118300 -12 31 10.396500
    catalog -> CIRS: 14 34 20.2370587 -12 34 36.381654
CIRS -> astrometric: 14 34 16.4960283 -12 31 02.523786
astrometric -> CIRS: 14 34 20.2370587 -12 34 36.381654
geocentric apparent: 14 35 01.7725801 -12 34 36.381654
CIRS -> topocentric: 14 34 20.2445622 -12 34 36.166337
    CIRS -> observed: 14 34 17.5776652 -12 36 29.928672
    ICRS -> observed: 14 34 17.5776655 -12 36 29.928667
ICRS -> CIRS (JPL, IERS): 14 34 20.2370639 -12 34 36.381756
ICRS -> CIRS (+ planets): 14 34 20.2370657 -12 34 36.381784
    CIRS -> astrometric: 14 34 16.4960283 -12 31 02.523786

```

---

Notes:

- The pressure value (731 hPa  $\equiv$  mB) is the actual pressure at the observer’s location, which aviators call QFE. A common mistake is to use QNH, the current pressure extrapolated down to sea level and consequently close to 1013 hPa irrespective of site altitude.
- The wavelength is in the yellow-green. To select the radio case, any number larger than 100 can be used.
- When starting from UTC, it is important to use the SOFA function `iauDtF2d` even though the result resembles an ordinary SOFA two-part JD: this is because of leap-second handling.
- The polar motion  $x$  and  $y$  can be set to zero in many low-accuracy applications. However, UT1–UTC is vital whenever topocentric or observed  $[h, \delta]$  or  $[az, alt]$  is being calculated.
- The example proper motion specifies both  $\mu_\alpha$  and  $\mu_\delta$  in milliarcseconds (per year), as in the Hipparcos catalog for example. The milliarcsecond unit identifies the  $\alpha$  proper motion component as being “distance on the sky” rather than “change in the right ascension coordinate”. The SOFA functions all use the latter, in common with the FK5 catalog for example, and so in the test case a  $\cos \delta$  scaling is required.

- The first result:

14<sup>h</sup> 34<sup>m</sup> 16<sup>s</sup>8118300 –12° 31′ 10″396500.

... is simply the supplied catalog  $[\alpha, \delta]$ .

- Next, the ICRS to (geocentric) CIRS transformation using the “single call” approach is demonstrated, in this case `iauAtci13`. The result is:

14<sup>h</sup> 34<sup>m</sup> 20<sup>s</sup>2370587 –12° 34′ 36″381654

If multiple stars were involved, and computational efficiency important, it would be better to call `iauApci13` once followed by multiple calls to `iauAtciq`.

- Next, the reverse transformation uses `iauAtic13` to give the “astrometric” place:

14<sup>h</sup> 34<sup>m</sup> 16<sup>s</sup>4960283 –12° 31′ 02″523786

This differs from the catalog  $[\alpha, \delta]$  in the first line of the report because the astrometric place includes the effects of the star’s proper motion from J2000.0 to date.

- The astrometric place is itself then transformed into CIRS by calling `iauAtci13` again, but this time with zero proper motion, parallax and radial velocity. The result...

14<sup>h</sup> 34<sup>m</sup> 20<sup>s</sup>2370587 –12° 34′ 36″381654

... is as before.

- Next, the classical (equinox based) apparent place is obtained, simply by taking the equation of the origins returned by the `iauAtci13` function and subtracting it from the (CIO based) CIRS  $\alpha$ , leaving  $\delta$  unchanged:

14<sup>h</sup> 35<sup>m</sup> 01<sup>s</sup>7725801 –12° 34′ 36″381654

- The CIRS position is transformed into topocentric  $[\alpha, \delta]$  by calling the CIRS  $\rightarrow$  observed `iauAtio13` function with zero air pressure:

14<sup>h</sup> 34<sup>m</sup> 20<sup>s</sup>:2445622–12° 34′ 36″.166337

- Calling `iauAtio13` function again but this time with the ambient conditions specified gives the observed  $[\alpha, \delta]$ :

14<sup>h</sup> 34<sup>m</sup> 17<sup>s</sup>:5776652–12° 36′ 29″.928672

- The two-stage transformation ICRS  $\rightarrow$  CIRS  $\rightarrow$  observed, although convenient in many applications, involves diurnal corrections that are non-rigorous. The `iauAtco13` function performs the direct ICRS  $\rightarrow$  observed transformation to reach this slightly different result:

14<sup>h</sup> 34<sup>m</sup> 17<sup>s</sup>:5776655–12° 36′ 29″.928667

- Next, the ICRS to CIRS transformation that we started with is repeated, but this time using the JPL DE405 solar-system ephemeris to obtain the Earth position and velocity, instead of the SOFA function `iauEpv00`, and using the CIP published in IERS bulletins. This is accomplished by performing the transformation in two steps, first by populating the astrometry context and then using it on the test target. This involves the functions `iauApci` followed by `iauAciq`. `iauApci` will require not just the barycentric vectors but also the heliocentric position, so the first step is to compute the Earth ephemeris using SOFA functions and then substitute the DE405 barycentric vector components: see the code for the numerical values. We obtain the best possible CIP by adding corrections  $dx, dy$  published by the IERS to their reference bias-precession-nutation model, namely IAU 2000A, and finally use SOFA to obtain the CIO locator  $s$ . We can then call `iauApci` specifying the mixture of SOFA/JPL/IERS data, followed by `iauAciq` to perform the transformation. The result is:

14<sup>h</sup> 34<sup>m</sup> 20<sup>s</sup>:2370639–12° 34′ 36″.381756

Almost all of the difference between this and the previous CIRS results is because of the IERS CIP corrections, which for the most part are to provide the (unmodeled) free core nutation. A very small contribution comes from the improved Earth velocity and its effect on the aberration, but this is never more than about  $5 \mu\text{as}$ .

- All the transformations up to now have taken into account the light deflection by the Sun, a refinement that on its own exceeds the accuracy demands of most applications. However, applications requiring the utmost accuracy should in addition take account of the planets, and to this end the example includes Jupiter and Saturn. For each of these bodies, plus the Sun, the code specifies the mass and the barycentric position and velocity at the epoch of observation; as before, values from DE405 are used. Also needed is a cutoff parameter, chosen to be within the disk of the body as seen by the observer, within which the calculation is suppressed to avoid numerical difficulties.

The transformation from catalog coordinates to CIRS is performed by an extended form of the `iauAtciq` function, namely `iauAtciqn` call. This requires two additional arguments, namely the number of solar-system bodies to be taken into account and an array of that many per-body parameter sets. In this example the order is Saturn then Jupiter then Sun. The result of the transformation is:

$14^{\text{h}} 34^{\text{m}} 20^{\text{s}}.2370657 - 12^{\circ} 34' 36''.381784$

The small differences with respect to the Sun-only calculation are, in this case, due to Saturn, which is about  $0^{\circ}38'$  from the star, compared with  $148^{\circ}$  and  $153^{\circ}$  for Jupiter and the Sun respectively.

- Finally, that result is transformed back into astrometric place. The result agrees with that obtained earlier:

$14^{\text{h}} 34^{\text{m}} 16^{\text{s}}.4960283 - 12^{\circ} 31' 02''.523786$

## 7 Alphabetical list of functions

A complete list of the SOFA astrometry functions<sup>4</sup> follows, arranged alphabetically. There are three main categories:

1. Those with names beginning `iauAp` populate a context structure with star-independent parameters that prepare the way for transformations on one or more targets. Various combinations of observer location and transformation type are provided for: it is vital to choose the right one for the job in hand: otherwise the results are undefined. The “populate” functions come in two sorts:
  - (a) Those with names ending in `13` are the most commonly used. The caller specifies data such as site coordinates, and other SOFA functions are then used internally to compute Earth ephemerides, precession-nutation, refraction constants and so on.
  - (b) The rest are “special”, in that they allow the caller to supply his own parameters, for instance looked up in a numerical ephemeris or calculated using a favorite refraction model.
2. Those functions with names beginning `iauAt` perform a particular transformation. There are two sorts of “transform” functions:
  - (a) Those names ending in `q` or `qz` are the “quick” functions that perform transformations using a pre-computed star-independent context. These are most useful when performing the same transformation on multiple targets.
  - (b) The others are single calls that perform the specified transformation on a single target.
3. The remaining functions support particular transformation steps.

To avoid unnecessary proliferation, not all combinations are supported. For example there are no “special” versions of the convenient one-call transformation functions: if the user wishes to use his own ephemeris, refraction, *etc.*, it will be necessary to use the two-call approach.

**Most applications will need only the handful of easy-to-use Type 2b functions.**

---

<sup>4</sup>All are classed as “support functions”: although they are meant to represent good practice, they do not claim to implement IAU standards or resolutions.

---

<b>iauAb</b>	<i>stellar aberration</i>	<b>iauAb</b>
--------------	---------------------------	--------------

**CALL :**

```
iauAb ( pnat, v, s, bm1, ppr );
```

**ACTION :**

Apply aberration to transform natural direction into proper direction.

**GIVEN :**

<i>pnat</i>	double	natural direction to the source (unit vector)
<i>v</i>	double[3]	<b>v</b> : observer barycentric velocity in units of c
<i>s</i>	double	distance between the Sun and the observer (au)
<i>bm1</i>	double	$(1 -  \mathbf{v} ^2)^{1/2}$ : reciprocal of Lorentz factor

**RETURNED :**

<i>ppr</i>	double[3]	proper direction to source (unit vector)
------------	-----------	--

**NOTES :**

1. The algorithm is based on Eq. (7.40) in the *Explanatory Supplement* (Urban & Seidelmann 2013), but with the following changes:
  - Rigorous rather than approximate normalization is applied.
  - The gravitational potential term from Eq. (7) in Klioner (2003) is added, taking into account only the Sun's contribution. This has a maximum effect of about  $0.4 \mu\text{as}$ .
2. In almost all cases, the maximum accuracy will be limited by the supplied velocity. For example, if the SOFA function `iauEpv00` is used, errors of up to  $5 \mu\text{as}$  could occur.

---

**iauApcg**                      *prepare for ICRS ↔ GCRS, geocentric, special*                      **iauApcg**

**CALL :**

```
iauApcg ( date1, date2, eb, eh, &astrom );
```

**ACTION :**

For a geocentric observer, prepare star-independent astrometry parameters for transformations between ICRS and GCRS coordinates. The Earth ephemeris is supplied by the caller.

**GIVEN :**

<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 1)
<i>eb</i>	double [2] [3]	Earth barycentric position/velocity (au, au/day)
<i>eh</i>	double [2] [3]	Earth heliocentric position/velocity (au, au/day)

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
---------------	------------	--

**NOTES :**

1. The TDB date *date1+date2* is a Julian Date, apportioned in any convenient way between the arguments *date1* and *date2*. For example,  $JD(TDB) = 2450123.7$  could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The J2000 method is best matched to the way the argument is handled internally and will deliver the optimum resolution. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

2. All the vectors are with respect to BCRS axes.
3. The context structure *astrom* produced by this function is used by *iauAtciq\** and *iauAticq\**.

---

**iauApcg13**                      *prepare for ICRS ↔ GCRS, geocentric*                      **iauApcg13**
**CALL :**

```
iauApcg13 ( date1, date2, &astrom );
```

**ACTION :**

For a geocentric observer, prepare star-independent astrometry parameters for transformations between ICRS and GCRS coordinates. The caller supplies the date, and SOFA models are used to predict the Earth ephemeris.

**GIVEN :**

<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 1)

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
---------------	------------	--

**NOTES :**

1. The TDB date *date1+date2* is a Julian Date, apportioned in any convenient way between the arguments *date1* and *date2*. For example,  $JD(TDB) = 2450123.7$  could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The J2000 method is best matched to the way the argument is handled internally and will deliver the optimum resolution. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

2. All the vectors are with respect to BCRS axes.
3. In cases where the caller wishes to supply his own Earth ephemeris, the function `iauApcg` can be used instead of the present function.
4. The context structure *astrom* produced by this function is used by `iauAtciq*` and `iauAticq*`.

---

**iauApci**                      *prepare for ICRS ↔ CIRS, terrestrial, special*                      **iauApci**

**CALL :**

```
iauApci ( date1, date2, eb, eh, x, y, s, &astrom );
```

**ACTION :**

For a terrestrial observer, prepare star-independent astrometry parameters for transformations between ICRS and geocentric CIRS coordinates. The Earth ephemeris and CIP/CIO are supplied by the caller.

**GIVEN :**

<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 1)
<i>eb</i>	double [2] [3]	Earth barycentric position/velocity (au, au/day)
<i>eh</i>	double [2] [3]	Earth heliocentric position/velocity (au, au/day)
<i>x,y</i>	double	CIP <i>X, Y</i> (components of unit vector)
<i>s</i>	double	the CIO locator <i>s</i> (radians)

**RETURNED :**

*ASTROM*    iauASTROM\*    star-independent astrometry parameters

**NOTES :**

1. The TDB date *date1+date2* is a Julian Date, apportioned in any convenient way between the arguments *date1* and *date2*. For example,  $JD(TDB) = 2450123.7$  could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

2. All the vectors are with respect to BCRS axes.
3. In cases where the caller does not wish to provide the Earth ephemeris and CIP/CIO, the function `iauApci13` can be used instead of the present function. This computes the required quantities using other SOFA functions.
4. The context structure *astrom* produced by this function is used by `iauAtciq*` and `iauAticq*`.

---

**iauApci13**                      *prepare for ICRS ↔ CIRS, terrestrial*                      **iauApci13**
**CALL :**

```
iauApci13 ( date1, date2, &astrom, &eo );
```

**ACTION :**

For a terrestrial observer, prepare star-independent astrometry parameters for transformations between ICRS and geocentric CIRS coordinates. The caller supplies the date, and SOFA models are used to predict the Earth ephemeris and CIP/CIO.

**GIVEN :**

<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 1)

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
<i>eo</i>	double*	equation of the origins (ERA–GST)

**NOTES :**

1. The TDB date *date1+date2* is a Julian Date, apportioned in any convenient way between the arguments *date1* and *date2*. For example,  $JD(TDB) = 2450123.7$  could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The J2000 method is best matched to the way the argument is handled internally and will deliver the optimum resolution. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

2. All the vectors are with respect to BCRS axes.
3. In cases where the caller wishes to supply his own Earth ephemeris and CIP/CIO, the function `iauApci` can be used instead of the present function.
4. The context structure *astrom* produced by this function is used by `iauAtciq*` and `iauAticq*`.

---

**iauApco**                    *prepare for ICRS ↔ observed, terrestrial, special*                    **iauApco**

**CALL :**

```
iauApco ( date1, date2, eb, eh, x, y, s,
          theta, elong, phi, hm, xp, yp, sp, refa, refb, &astrom );
```

**ACTION :**

For a terrestrial observer, prepare star-independent astrometry parameters for transformations between ICRS and observed coordinates. The caller supplies the Earth ephemeris, the Earth rotation information and the refraction constants as well as the site coordinates.

**GIVEN :**

<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 1)
<i>eb</i>	double[2] [3]	Earth barycentric pos/vel (au, au/day, Note 2)
<i>eh</i>	double[2] [3]	Earth heliocentric pos/vel (au, au/day, Note 2)
<i>x,y</i>	double	CIP X, Y (components of unit vector)
<i>s</i>	double	the CIO locator <i>s</i> (radians)
<i>theta</i>	double	Earth rotation angle (radians)
<i>elong</i>	double	longitude (radians, east-positive, Note 3)
<i>phi</i>	double	latitude (geodetic, radians, Note 3)
<i>hm</i>	double	height above ellipsoid (m, geodetic, Note 3)
<i>xp,yp</i>	double	polar motion coordinates (radians, Note 4)
<i>sp</i>	double	the TIO locator <i>s'</i> (radians, Note 4)
<i>refa</i>	double	refraction constant A (radians, Note 5)
<i>refb</i>	double	refraction constant B (radians, Note 5)

**RETURNED :**

*astrom*            iauASTROM\*    star-independent astrometry parameters

**NOTES :**

1. The TDB date *date1+date2* is a Julian Date, apportioned in any convenient way between the arguments *date1* and *date2*. For example, JD(TDB) = 2450123.7 could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

2. The vectors *eb*, *eh*, and all the *astrom* vectors, are with respect to BCRS axes.
3. The geographical coordinates are with respect to the WGS84 reference ellipsoid. **Take care with the longitude sign:** the longitude required by the present function is east-positive (*i.e.* right-handed), in accordance with geographical convention.
4. The polar motion *xp,yp* can be obtained from IERS bulletins. The values are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System (see IERS Conventions 2003), measured along the meridians 0° and 90° west respectively. For many applications, *xp* and *yp* can be set to zero.
5. The refraction constants *refa* and *refb* are for use in a  $\Delta\zeta = A \tan \zeta + B \tan^3 \zeta$  model, where  $\zeta$  is the observed (*i.e.* refracted) zenith distance and  $\Delta\zeta$  is the amount of refraction.
6. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.
7. In cases where the caller does not wish to provide the Earth Ephemeris, the Earth rotation information and refraction constants, the function `iauApco13` can be used instead of the present function. This starts from UTC and weather readings *etc.* and computes suitable values using other SOFA functions.
8. The context structure *astrom* produced by this function is used by `iauAtioq`, `iauAtoiq`, `iauAtciq*` and `iauAticq*`.

---

**iauApcol3**                      *prepare for ICRS ↔ observed, terrestrial*                      **iauApcol3**

**CALL :**

```
status = iauApcol3 ( utc1, utc2, dut1, elong, phi, hm, xp, yp,
                   phpa, tc, rh, wl, &astrom, &eo );
```

**ACTION :**

For a terrestrial observer, prepare star-independent astrometry parameters for transformations between ICRS and observed coordinates. The caller supplies UTC, site coordinates, ambient air conditions and observing wavelength, and SOFA models are used to obtain the Earth ephemeris, CIP/CIO and refraction constants.

**GIVEN :**

<i>utc1</i>	double	UTC as a 2-part...
<i>utc2</i>	double	... quasi Julian Date (Notes 1,2)
<i>dut1</i>	double	UT1–UTC (seconds)
<i>elong</i>	double	longitude (radians, east-positive, Note 3)
<i>phi</i>	double	geodetic latitude (radians, Note 3)
<i>hm</i>	double	height above ellipsoid (m, geodetic Notes 4,6)
<i>xp,yp</i>	double	polar motion coordinates (radians, Note 5)
<i>phpa</i>	double	pressure at the observer (hPa ≡ mB, Note 6)
<i>tc</i>	double	ambient temperature at the observer (deg C)
<i>rh</i>	double	relative humidity at the observer (range 0-1)
<i>wl</i>	double	wavelength (micrometers, Note 7)

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
<i>eo</i>	double*	equation of the origins (ERA–GST)

**RETURNED** (function value) :

<b>int</b>	status:	+1 = dubious year (Note 2)
		0 = OK
		-1 = unacceptable date

**NOTES :**

1. *utc1+utc2* is quasi Julian Date (see Note 2), apportioned in any convenient way between the two arguments, for example where *utc1* is the Julian Day Number and *utc2* is the fraction of a day. However, JD cannot unambiguously represent UTC during a leap second unless special measures are taken. The convention in the present function is that the JD day represents UTC days whether the length is 86399, 86400 or 86401 SI seconds.

Applications should use the function `iauDtfd` to convert from calendar date and time of day into two-part quasi Julian Date, as it implements the leap-second-ambiguity convention just described.

2. The warning status “dubious year” flags UTCs that predate the introduction of the time scale or that are too far in the future to be trusted. See `iauDat` for further details.
3. UT1–UTC is tabulated in IERS bulletins. It increases by exactly one second at the end of each positive UTC leap second, introduced in order to keep UT1–UTC within  $\pm 0.9$  s. *n.b.* This practice is under review, and in the future UT1–UTC may grow essentially without limit.
4. The geographical coordinates are with respect to the WGS84 reference ellipsoid. **Take care with the longitude sign:** the longitude required by the present function is east-positive (*i.e.* right-handed), in accordance with geographical convention.
5. The polar motion  $xp, yp$  can be obtained from IERS bulletins. The values are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System (see IERS Conventions 2003), measured along the meridians  $0^\circ$  and  $90^\circ$  west respectively. For many applications,  $xp$  and  $yp$  can be set to zero.
6. If  $h$ , the height above the ellipsoid of the observing station in meters, is not known but  $p$ , the pressure in hPa ( $\equiv$ mB), is available, an adequate estimate of  $h$  can be obtained from the expression

$$h = -29.3 t_0 \log(p/1013.25)$$

where  $t_0$  is the approximate sea-level air temperature in K (See *Astrophysical Quantities*, C.W. Allen, 3rd edition, Section 52). Similarly, if the pressure  $p$  is not known, it can be estimated from the height of the observing station,  $h$ , as follows:

$$p = 1013.25 e^{-h/(29.3t_0)}$$

Note, however, that the refraction is nearly proportional to the pressure and that an accurate  $p$  value is important for precise work.

7. The argument  $wl$  specifies the observing wavelength in micrometers. The transition from optical to radio is assumed to occur at  $100 \mu\text{m}$  (about 3000 GHz).
8. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.
9. In cases where the caller wishes to supply his own Earth ephemeris, Earth rotation information and refraction constants, the function `iauApco` can be used instead of the present function.
10. The context structure `astrom` produced by this function is used by `iauAtioq`, `iauAtoiq`, `iauAtciq*` and `iauAticq*`.

---

**iauApcs**                      *prepare for ICRS ↔ GCRS, space, special*                      **iauApcs**

**CALL :**

```
iauApcs ( date1, date2, pv, eb, eh, &astrom );
```

**ACTION :**

For an observer whose geocentric position and velocity are known, prepare star-independent astrometry parameters for transformations between ICRS and GCRS. The Earth ephemeris is supplied by the caller.

**GIVEN :**

<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 1)
<i>pv</i>	double [2] [3]	observer's geocentric pos/vel (m, m/s)
<i>eb</i>	double [2] [3]	Earth barycentric pos/vel (au, au/day)
<i>eh</i>	double [2] [3]	Earth heliocentric pos/vel (au, au/day)

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
---------------	------------	--

**NOTES :**

1. The TDB date *date1+date2* is a Julian Date, apportioned in any convenient way between the arguments *date1* and *date2*. For example,  $JD(TDB) = 2450123.7$  could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The J2000 method is best matched to the way the argument is handled internally and will deliver the optimum resolution. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

2. All the vectors are with respect to BCRS axes.
3. Providing separate arguments for (i) the observer's geocentric position and velocity and (ii) the Earth ephemeris is done for convenience in the geocentric, terrestrial and Earth orbit cases. For deep space applications it maybe more convenient to specify zero geocentric position and velocity and to supply the observer's position and velocity information directly instead of with respect to the Earth. However, note the different units: m and m/s for the geocentric vectors, au and au/day for the heliocentric and barycentric vectors.

4. In cases where the caller does not wish to provide the Earth ephemeris, the function `iauApcs13` can be used instead of the present function. This computes the Earth ephemeris using the SOFA function `iauEpv00`.
5. The context structure `astrom` produced by this function is used by `iauAtciq*` and `iauAticq*`.

---

**iauApcs13** *prepare for ICRS ↔ CIRS, space* **iauApcs13**


---

**CALL :**

```
iauApcs13 ( date1, date2, pv, &astrom );
```

**ACTION :**

For an observer whose geocentric position and velocity are known, prepare star-independent astrometry parameters for transformations between ICRS and GCRS. The Earth ephemeris is from SOFA models.

**GIVEN :**

<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 1)
<i>pv</i>	double[2] [3]	observer's geocentric position/velocity (Note 3)

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
---------------	------------	--

**NOTES :**

1. The TDB date *date1+date2* is a Julian Date, apportioned in any convenient way between the arguments *date1* and *date2*. For example, JD(TDB) = 2450123.7 could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The J2000 method is best matched to the way the argument is handled internally and will deliver the optimum resolution. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

2. All the vectors are with respect to BCRS axes.
3. The observer's position and velocity *pv* are geocentric but with respect to BCRS axes, and in units of m and m/s. No assumptions are made about proximity to the Earth, and the function can be used for deep space applications as well as Earth orbit and terrestrial.
4. In cases where the caller wishes to supply his own Earth ephemeris, the function **iauApcs** can be used instead of the present function.
5. The context structure *astrom* produced by this function is used by **iauAtciq\*** and **iauAticq\***.

---

**iauAper***insert ERA into context***iauAper****CALL :**

```
iauAper ( theta, &astrom );
```

**ACTION :**

In the star-independent astrometry parameters, update only the Earth rotation angle, supplied by the caller explicitly.

**GIVEN :**

<i>theta</i>	double	Earth rotation angle (radians, Note 2)
<i>astrom</i>	iauASTROM*	star-independent astrometry parameters

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
---------------	------------	--

**NOTES :**

1. This function exists to enable sidereal-tracking applications to avoid wasteful re-computation of the bulk of the astrometry parameters: only the Earth rotation is updated.
2. For targets expressed as equinox based positions, such as classical geocentric apparent  $[\alpha, \delta]$ , the supplied *theta* can be Greenwich apparent sidereal time rather than Earth rotation angle.
3. The function `iauAper13` can be used instead of the present function, and starts from UT1 rather than ERA itself.

---

**iauAper13**                      *update context for Earth rotation*                      **iauAper13**

**CALL :**

```
iauAper13 ( ut11, ut12, &astrom );
```

**ACTION :**

In the star-independent astrometry parameters, update only the Earth rotation angle: the caller provides UT1 (*n.b.* not UTC) and the IAU 2000 ERA formula is used.

**GIVEN :**

<i>ut11</i>	double	UT1 as a 2-part...
<i>ut12</i>	double	... Julian Date (Note 1)
<i>astrom</i>	iauASTROM*	star-independent astrometry parameters

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
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**NOTES :**

1. The UT1 date  $ut11+ut12$  is a Julian Date, apportioned in any convenient way between the arguments  $ut11$  and  $ut12$ . For example,  $JD(UT1) = 2450123.7$  could be expressed in any of these ways, among others:

<i>ut11</i>	<i>ut12</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The J2000 and MJD methods are good compromises between resolution and convenience. The date & time method is best matched to the algorithm used: maximum precision is delivered when the  $ut11$  argument is for  $0^h$  UT1 on the day in question and the  $ut12$  argument lies in the range 0 to 1, or *vice versa*.

2. If the caller wishes to provide the Earth rotation angle itself, the function `iauAper` can be used instead. One use of this technique is to substitute Greenwich apparent sidereal time and thereby to support equinox based transformations directly.

---

**iauApio**                      *prepare for CIRS ↔ observed, terrestrial, special*                      **iauApio**

**CALL :**

```
iauApio ( sp, theta, elong, phi, hm, xp, yp, refa, refb, &astrom );
```

**ACTION :**

For a terrestrial observer, prepare star-independent astrometry parameters for transformations between CIRS and observed coordinates. The caller supplies the Earth orientation information and the refraction constants as well as the site coordinates.

**GIVEN :**

<i>sp</i>	double	the TIO locator $s'$ (radians, Note 1)
<i>theta</i>	double	Earth rotation angle (radians)
<i>elong</i>	double	longitude (radians, east-positive, Note 2)
<i>phi</i>	double	geodetic latitude (radians, Note 2)
<i>hm</i>	double	height above ellipsoid (m, geodetic Note 2)
<i>xp,yp</i>	double	polar motion coordinates (radians, Note 3)
<i>refa</i>	double	refraction constant $A$ (radians, Note 4)
<i>refb</i>	double	refraction constant $B$ (radians, Note 4)

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
---------------	------------	--

**NOTES :**

1. *sp*, the TIO locator  $s'$ , is a tiny quantity needed only by the most precise applications. It can either be set to zero or predicted using the SOFA function `iauSp00`.
2. The geographical coordinates are with respect to the WGS84 reference ellipsoid. **Take care with the longitude sign:** the longitude required by the present function is east-positive (*i.e.* right-handed), in accordance with geographical convention.
3. The polar motion *xp,yp* can be obtained from IERS bulletins. The values are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System (see IERS Conventions 2003), measured along the meridians  $0^\circ$  and  $90^\circ$  west respectively. For many applications, *xp* and *yp* can be set to zero.
4. The refraction constants *refa* and *refb* are for use in a  $\Delta\zeta = A \tan \zeta + B \tan^3 \zeta$  model, where  $\zeta$  is the observed (*i.e.* refracted) zenith distance and  $\Delta\zeta$  is the amount of refraction.
5. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.
6. In cases where the caller does not wish to provide the Earth rotation information and refraction constants, the function `iauApio13` can be used instead of the present function. This starts from UTC and weather readings *etc.* and computes suitable values using other SOFA functions.
7. The context structure *astrom* produced by this function is used by `iauAtioq` and `iauAtoiq`.

---

**iauApio13**                      *prepare for CIRS ↔ observed, terrestrial*                      **iauApio13**


---

**CALL :**

```
status = iauApio13 ( utc1, utc2, dut1, elong, phi, hm, xp, yp,
                    phpa, tc, rh, wl, &astrom );
```

**ACTION :**

For a terrestrial observer, prepare star-independent astrometry parameters for transformations between CIRS and observed coordinates. The caller supplies UTC, site coordinates, ambient air conditions and observing wavelength.

**GIVEN :**

<i>utc1</i>	double	UTC as a 2-part...
<i>utc2</i>	double	...quasi Julian Date (Notes 1,2)
<i>dut1</i>	double	UT1–UTC (seconds)
<i>elong</i>	double	longitude (radians, east-positive, Note 3)
<i>phi</i>	double	geodetic latitude (radians, Note 3)
<i>hm</i>	double	height above ellipsoid (m, geodetic Notes 4,6)
<i>xp,yp</i>	double	polar motion coordinates (radians, Note 5)
<i>phpa</i>	double	pressure at the observer (hPa ≡ mB, Note 6)
<i>tc</i>	double	ambient temperature at the observer (deg C)
<i>rh</i>	double	relative humidity at the observer (range 0-1)
<i>wl</i>	double	wavelength (micrometers, Note 7)

**RETURNED :**

<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
---------------	------------	--

**RETURNED** (function value) :

int	status:	+1 = dubious year (Note 2)
		0 = OK
		-1 = unacceptable date

**NOTES :**

1. *utc1+utc2* is quasi Julian Date (see Note 2), apportioned in any convenient way between the two arguments, for example where *utc1* is the Julian Day Number and *utc2* is the fraction of a day. However, JD cannot unambiguously represent UTC during a leap second unless special measures are taken. The convention in the present function is that the JD day represents UTC days whether the length is 86399, 86400 or 86401 SI seconds.

Applications should use the function `iauDtfd` to convert from calendar date and time of day into two-part quasi Julian Date, as it implements the leap-second-ambiguity convention just described.

2. The warning status “dubious year” flags UTCs that predate the introduction of the time scale or that are too far in the future to be trusted. See `iauDat` for further details.
3. UT1–UTC is tabulated in IERS bulletins. It increases by exactly one second at the end of each positive UTC leap second, introduced in order to keep UT1–UTC within  $\pm 0.9$  s. *n.b.* This practice is under review, and in the future UT1–UTC may grow essentially without limit.
4. The geographical coordinates are with respect to the WGS84 reference ellipsoid. **Take care with the longitude sign:** the longitude required by the present function is east-positive (*i.e.* right-handed), in accordance with geographical convention.
5. The polar motion  $xp, yp$  can be obtained from IERS bulletins. The values are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System (see IERS Conventions 2003), measured along the meridians  $0^\circ$  and  $90^\circ$  west respectively. For many applications,  $xp$  and  $yp$  can be set to zero.
6. If  $h$ , the height above the ellipsoid of the observing station in meters, is not known but  $p$ , the pressure in hPa ( $\equiv$ mB), is available, an adequate estimate of  $h$  can be obtained from the expression

$$h = -29.3 t_0 \log(p/1013.25)$$

where  $t_0$  is the approximate sea-level air temperature in K (See *Astrophysical Quantities*, C.W. Allen, 3rd edition, Section 52). Similarly, if the pressure  $p$  is not known, it can be estimated from the height of the observing station,  $h$ , as follows:

$$p = 1013.25 e^{-h/(29.3t_0)}$$

Note, however, that the refraction is nearly proportional to the pressure and that an accurate  $p$  value is important for precise work.

7. The argument  $wl$  specifies the observing wavelength in micrometers. The transition from optical to radio is assumed to occur at  $100 \mu\text{m}$  (about 3000 GHz).
8. The observer’s geocentric position/velocity are with respect to GCRS.
9. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.
10. In cases where the caller wishes to supply his own Earth rotation information and refraction constants, the function `iauApio` can be used instead of the present function.
11. The context structure `astrom` produced by this function is used by `iauAtioq` and `iauAtoiq`.

---

**iauAtci13** *catalog* → *CIRS* **iauAtci13**
**CALL :**

```
iauAtci13 ( rc, dc, pr, pd, px, rv, date1, date2, &ri, &di, &eo );
```

**ACTION :**

Transform ICRS star data, epoch J2000.0, to CIRS.

**GIVEN :**

<i>rc, dc</i>	double	ICRS [ $\alpha, \delta$ ] at J2000.0 (radians, Note 1)
<i>pr</i>	double	RA proper motion (radians/year; Note 2)
<i>pd</i>	double	Dec proper motion (radians/year)
<i>px</i>	double	parallax (arcsec)
<i>rv</i>	double	radial velocity (km/s, positive if receding)
<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 3)

**RETURNED :**

<i>ri, di</i>	double*	CIRS geocentric [ $\alpha, \delta$ ] (radians)
<i>eo</i>	double*	equation of the origins (ERA–GST, Note 5)

**NOTES :**

1. Star data for an epoch other than J2000.0 (for example from the Hipparcos catalog, which has an epoch of J1991.25) will require a preliminary call to `iauPmsafe` before use.
2. The proper motion in right ascension is  $\dot{\alpha}$  rather than  $\dot{\alpha} \cos \delta$ .
3. The TDB date  $date1 + date2$  is a Julian Date, apportioned in any convenient way between the arguments  $date1$  and  $date2$ . For example,  $JD(TDB) = 2450123.7$  could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The J2000 method is best matched to the way the argument is handled internally and will deliver the optimum resolution. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

4. Should the transformation to (equinox based) apparent place be required rather than (CIO based) intermediate place, subtract the equation of the origins from the returned right ascension:  $\alpha_{\text{apparent}} = \alpha_{\text{CIRS}} - eo$ . (The `iauAnp` function can then be applied, as required, to keep the result in the conventional 0- $2\pi$  range.)

---

**iauAtciq***quick ICRS* → *CIRS***iauAtciq****CALL :**

```
iauAtciq ( rc, dc, pr, pd, px, rv, &astrom, &ri, &di );
```

**ACTION :**

Quick ICRS, epoch J2000.0, to CIRS transformation, given precomputed star-independent astrometry parameters. Use of this function is appropriate when efficiency is important and where many star positions are to be transformed for one date.

**GIVEN :**

<i>rc,dc</i>	double	ICRS [ $\alpha, \delta$ ] at J2000.0 (radians, Note 1)
<i>pr</i>	double	RA proper motion (radians/year; Note 2)
<i>pd</i>	double	Dec proper motion (radians/year)
<i>px</i>	double	parallax (arcsec)
<i>rv</i>	double	radial velocity (km/s, positive if receding)
<i>astrom</i>	iauASTROM*	star-independent astrometry parameters

**RETURNED :**

<i>ri,di</i>	double*	CIRS geocentric [ $\alpha, \delta$ ] (radians)
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**NOTES :**

1. Star data for an epoch other than J2000.0 (for example from the Hipparcos catalog, which has an epoch of J1991.25) will require a preliminary call to `iauPmsafe` before use.
2. The proper motion in right ascension is  $\dot{\alpha}$  rather than  $\dot{\alpha} \cos \delta$ .
3. If the parallax and proper motions are zero (or the supplied [ $\alpha, \delta$ ] is an astrometric place) the `iauAtciqz` function can be used instead.
4. The star-independent parameters can be obtained by calling one of the functions `iauApci[13]`, `iauApcg[13]`, `iauApco[13]` or `iauApcs[13]`.

---

**iauAtciqn**                      *quick ICRS* → *CIRS*, *multiple deflections*                      **iauAtciqn**

**CALL :**

```
iauAtciqn ( rc, dc, pr, pd, px, rv, astrom, n, b, &ri, &di );
```

**ACTION :**

Quick ICRS, epoch J2000.0, to CIRS transformation, given precomputed star-independent astrometry parameters plus a list of light-deflecting bodies. Use of this function is appropriate when efficiency is important and where many star positions are to be transformed for one date.

**GIVEN :**

<i>rc, dc</i>	double	ICRS [ $\alpha, \delta$ ] at J2000.0 (radians, Note 1)
<i>pr</i>	double	RA proper motion (radians/year; Note 2)
<i>pd</i>	double	Dec proper motion (radians/year)
<i>px</i>	double	parallax (arcsec)
<i>rv</i>	double	radial velocity (km/s, positive if receding)
<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
<i>n</i>	int	number of bodies (Note 5)
<i>b</i>	iauLDBODY[n]	data for each of the <i>n</i> bodies (Notes 5-9)

**RETURNED :**

<i>ri, di</i>	double*	CIRS geocentric [ $\alpha, \delta$ ] (radians)
---------------	---------	--

**NOTES :**

1. Star data for an epoch other than J2000.0 (for example from the Hipparcos catalog, which has an epoch of J1991.25) will require a preliminary call to `iauPmsafe` before use.
2. The proper motion in right ascension is  $\dot{\alpha}$  rather than  $\dot{\alpha} \cos \delta$ .
3. If the only light-deflecting body to be taken into account is the Sun, the `iauAtciq` function can be used instead. If in addition the parallax and proper motions are zero, the `iauAtciqz` function can be used.
4. The star-independent parameters can be obtained by calling one of the functions `iauApci[13]`, `iauApcg[13]`, `iauApco[13]` or `iauApcs[13]`.
5. The array *b* contains *n* entries, one for each body to be considered. If *n* = 0, no gravitational light deflection will be applied, not even for the Sun.
6. The array *b* should include an entry for the Sun as well as for any planet or other body to be taken into account. The entries should be in the order in which the light passes the body.

7. In the entry in the  $b$  array for body  $i$ , the mass parameter  $b[i-1].bm$  can, as required, be adjusted in order to allow for such effects as quadrupole field.
8. The deflection limiter parameter  $b[i].dl$  is  $\phi^2/2$ , where  $\phi$  is the angular separation (in radians) between star and body at which limiting is applied. As  $\phi$  shrinks below the chosen threshold, the deflection is artificially reduced, reaching zero for  $\phi = 0$ . Example values suitable for a terrestrial observer, together with masses, are as follows:

body $i$	$b[i-1].bm$	$b[i-1].dl$
Sun	1.0	6e-6
Jupiter	0.00095435	3e-9
Saturn	0.00028574	3e-10

9. For efficiency, validation of the contents of the  $b$  array is omitted. The supplied masses must be greater than zero, the position and velocity vectors must be right, and the deflection limiter greater than zero.

---

**iauAtciqz**                      *quick astrometric ICRS → CIRS*                      **iauAtciqz**

**CALL :**

```
iauAtciqz ( rc, dc, &astrom, &ri, &di );
```

**ACTION :**

Quick ICRS to CIRS transformation, given precomputed star-independent astrometry parameters, and assuming zero parallax and proper motion (*i.e.* astrometric place). Use of this function is appropriate when efficiency is important and where many star positions, all with parallax and proper motion either zero or already allowed for, are to be transformed for one date.

**GIVEN :**

<i>rc,dc</i>	double	ICRS $[\alpha, \delta]$
<i>astrom</i>	iauASTROM*	star-independent astrometry parameters

**RETURNED :**

<i>ri,di</i>	double*	CIRS geocentric $[\alpha, \delta]$ (radians)
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**NOTES :**

1. The corresponding function for the case of non-zero parallax and proper motion is `iauAtciq`.
2. The star-independent parameters can be obtained by calling one of the functions `iauApci[13]`, `iauApcg[13]`, `iauApco[13]` or `iauApcs[13]`.

**iauAtco13***ICRS* → *observed***iauAtco13****CALL :**

```
status = iauAtco13 ( rc, dc, pr, pd, px, rv, utc1, utc2, dut1,
                    elong phi, hm, xp, yp, phpa, tc, rh, wl,
                    aob, zob, hob, dob, rob, eo );
```

**ACTION :**

ICRS  $[\alpha, \delta]$  to observed place. The caller supplies UTC, site coordinates, ambient air conditions and observing wavelength.

**GIVEN :**

<i>rc, dc</i>	double	ICRS $[\alpha, \delta]$ at J2000.0 (radians, Note 1)
<i>pr</i>	double	RA proper motion (radians/year; Note 2)
<i>pd</i>	double	Dec proper motion (radians/year)
<i>px</i>	double	parallax (arcsec)
<i>rv</i>	double	radial velocity (km/s, positive if receding)
<i>utc1</i>	double	UTC as a 2-part...
<i>utc2</i>	double	... quasi Julian Date (Notes 3,4)
<i>dut1</i>	double	UT1–UTC (seconds, Note 5)
<i>elong</i>	double	longitude (radians, east-positive, Note 6)
<i>phi</i>	double	geodetic latitude (radians, Note 6)
<i>hm</i>	double	height above ellipsoid (m, geodetic Notes 6,8)
<i>xp, yp</i>	double	polar motion coordinates (radians, Note 7)
<i>phpa</i>	double	pressure at the observer (hPa $\equiv$ mB, Note 8)
<i>tc</i>	double	ambient temperature at the observer (deg C)
<i>rh</i>	double	relative humidity at the observer (range 0-1)
<i>wl</i>	double	wavelength (micrometers, Note 9)

**RETURNED :**

<i>aob</i>	double*	observed azimuth (radians: N=0°, E=90°)
<i>zob</i>	double*	observed zenith distance (radians)
<i>hob</i>	double*	observed hour angle (radians)
<i>dob</i>	double*	observed declination (radians)
<i>rob</i>	double*	observed right ascension (CIO-based, radians)
<i>eo</i>	double*	equation of the origins (ERA–GST)

**RETURNED** (function value) :

<b>int</b>	status:	+1 = dubious year (Note 2)
		0 = OK
		-1 = unacceptable date

## NOTES :

1. Star data for an epoch other than J2000.0 (for example from the Hipparcos catalog, which has an epoch of J1991.25) will require a preliminary call to `iauPmsafe` before use.
2. The proper motion in right ascension is  $\dot{\alpha}$  rather than  $\dot{\alpha} \cos \delta$ .
3. `utc1+utc2` is quasi Julian Date (see Note 2), apportioned in any convenient way between the two arguments, for example where `utc1` is the Julian Day Number and `utc2` is the fraction of a day. However, JD cannot unambiguously represent UTC during a leap second unless special measures are taken. The convention in the present function is that the JD day represents UTC days whether the length is 86399, 86400 or 86401 SI seconds.

Applications should use the function `iauDtfd2d` to convert from calendar date and time of day into two-part quasi Julian Date, as it implements the leap-second-ambiguity convention just described.

4. The warning status “dubious year” flags UTCs that predate the introduction of the time scale or that are too far in the future to be trusted. See `iauDat` for further details.
5. UT1–UTC is tabulated in IERS bulletins. It increases by exactly one second at the end of each positive UTC leap second, introduced in order to keep UT1–UTC within  $\pm 0.9$ s. *n.b.* This practice is under review, and in the future UT1–UTC may grow essentially without limit.
6. The geographical coordinates are with respect to the WGS84 reference ellipsoid. **Take care with the longitude sign:** the longitude required by the present function is east-positive (*i.e.* right-handed), in accordance with geographical convention.
7. The polar motion  $xp, yp$  can be obtained from IERS bulletins. The values are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System (see IERS Conventions 2003), measured along the meridians  $0^\circ$  and  $90^\circ$  west respectively. For many applications,  $xp$  and  $yp$  can be set to zero.
8. If  $h$ , the height above the ellipsoid of the observing station in meters, is not known but  $p$ , the pressure in hPa ( $\equiv$ mB), is available, an adequate estimate of  $h$  can be obtained from the expression

$$h = -29.3 t_0 \log(p/1013.25)$$

where  $t_0$  is the approximate sea-level air temperature in K (See *Astrophysical Quantities*, C.W. Allen, 3rd edition, Section 52). Similarly, if the pressure  $p$  is not known, it can be estimated from the height of the observing station,  $h$ , as follows:

$$p = 1013.25 e^{-h/(29.3t_0)}$$

Note, however, that the refraction is nearly proportional to the pressure and that an accurate  $p$  value is important for precise work.

9. The argument  $wl$  specifies the observing wavelength in micrometers. The transition from optical to radio is assumed to occur at  $100\ \mu\text{m}$  (about 3000 GHz).
10. “Observed” azimuth and zenith distance means the position that would be seen by a perfect geodetically aligned theodolite. (Zenith distance is used rather than altitude in order to reflect the fact that no allowance is made for depression of the horizon.) This is related to the observed  $[h, \delta]$  *via* the standard rotation, using the geodetic latitude (corrected for polar motion), while the observed  $h$  and  $\alpha$  are related simply through the Earth rotation angle and the site longitude. “Observed”  $[\alpha, \delta]$  or  $[h, \delta]$  thus means the position that would be seen by a perfect equatorial with its polar axis aligned to the Earth’s axis of rotation.
11. The accuracy of the result is limited by the corrections for refraction, which use a simple  $A \tan \zeta + B \tan^3 \zeta$  model. Providing the meteorological parameters are known accurately and there are no gross local effects, the predicted observed coordinates should be within  $0''.05$  (optical)  $1''$  (radio) for  $\zeta < 70^\circ$ , better than  $30''$  (optical or radio) at  $85^\circ$  and better than  $0''.3$  (optical) or  $0''.5$  (radio) at the horizon.

Without refraction, the complementary functions `iauAtco13` and `iauAtoc13` are self-consistent to better than  $1\ \mu\text{as}$  all over the celestial sphere. With refraction included, consistency falls off at high zenith distances, but is still better than  $0''.05$  at  $\zeta = 85^\circ$ .

12. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.

**iauAtic13***CIRS* → *ICRS***iauAtic13****CALL :**

```
iauAtic13 ( ri, di, date1, date2, &rc, &dc, &eo );
```

**ACTION :**

Transform  $[\alpha, \delta]$  from geocentric CIRS to ICRS astrometric.

**GIVEN :**

<i>ri, di</i>	double	CIRS geocentric $[\alpha, \delta]$ (radians)
<i>date1</i>	double	TDB as a 2-part...
<i>date2</i>	double	... Julian Date (Note 1)

**RETURNED :**

<i>rc, dc</i>	double*	ICRS astrometric $[\alpha, \delta]$
<i>eo</i>	double*	equation of the origins (ERA–GST, Note 4)

**NOTES :**

1. The TDB date *date1+date2* is a Julian Date, apportioned in any convenient way between the arguments *date1* and *date2*. For example,  $\text{JD}(\text{TDB}) = 2450123.7$  could be expressed in any of these ways, among others:

<i>date1</i>	<i>date2</i>	
2450123.7	0.0	(JD method)
2451545.0	-1421.3	(J2000 method)
2400000.5	50123.2	(MJD method)
2450123.5	0.2	(date & time method)

The JD method is the most natural and convenient to use in cases where the loss of several decimal digits of resolution is acceptable. The J2000 method is best matched to the way the argument is handled internally and will deliver the optimum resolution. The MJD method and the date & time methods are both good compromises between resolution and convenience. For most applications of this function the choice will not be at all critical.

**TT can be used instead of TDB without any significant impact on accuracy.**

2. Iterative techniques are used for the aberration and light deflection corrections so that the functions *iauAtic13* (or *iauAticq*) and *iauAtci13* (or *iauAtciq*) are accurate inverses; even at the edge of the Sun's disk the discrepancy is only about 1 nanoarcsecond.
3. Should the transformation to (equinox based) J2000.0 mean place be required rather than (CIO based) ICRS coordinates, subtract the equation of the origins from the returned right ascension:  $\alpha_{\text{apparent}} = \alpha_{\text{CIRS}} - eo$ . (The *iauAnp* function can then be applied, as required, to keep the result in the conventional  $0-2\pi$  range.)

---

**iauAticq***quick CIRS* → *ICRS***iauAticq****CALL :**

```
iauAticq ( ri, di, &astrom, &rc, &dc );
```

**ACTION :**

Quick CIRS to ICRS astrometric place transformation, given the star-independent astrometry parameters. Use of this function is appropriate when efficiency is important and where many star positions are all to be transformed for one date.

**GIVEN :**

<i>ri, di</i>	double	CIRS geocentric $[\alpha, \delta]$ (radians)
<i>astrom</i>	iauASTROM*	star-independent astrometry parameters

**RETURNED :**

<i>rc, dc</i>	double*	ICRS astrometric $[\alpha, \delta]$
---------------	---------	-------------------------------------

**NOTES :**

1. Only the Sun is taken into account in the light deflection correction.
2. Iterative techniques are used for the aberration and light deflection corrections so that the functions `iauAtic13` (or `iauAticq`) and `iauAtci13` (or `iauAtciq`) are accurate inverses; even at the edge of the Sun's disk the discrepancy is only about 1 nanoarcsecond.
3. The star-independent astrometry parameters can be obtained by calling one of the functions `iauApci[13]`, `iauApcg[13]`, `iauApco[13]` or `iauApcs[13]`.

---

**iauAtciqn**                      *quick CIRS* → *ICRS*, *multiple deflections*                      **iauAtciqn**

**CALL :**

```
iauAtciqn ( ri, di, astrom, n, b, &rc, &dc );
```

**ACTION :**

Quick CIRS to ICRS astrometric place transformation, given precomputed star-independent astrometry parameters plus a list of light-deflecting bodies. Use of this function is appropriate when efficiency is important and where many star positions are to be transformed for one date.

**GIVEN :**

<i>ri, di</i>	double	CIRS [ $\alpha, \delta$ ] (radians)
<i>astrom</i>	iauASTROM*	star-independent astrometry parameters
<i>n</i>	int	number of bodies (Note 4)
<i>b</i>	iauLDBODY[n]	data for each of the <i>n</i> bodies (Notes 4-8)

**RETURNED :**

<i>rc, dc</i>	double*	ICRS astrometric [ $\alpha, \delta$ ] (radians)
---------------	---------	---

**NOTES :**

1. Iterative techniques are used for the aberration and light deflection corrections so that the functions `iauAticqn` and `iauAtciqn` are accurate inverses; even at the edge of the Sun's disk the discrepancy is only about 1 nanoarcsecond.
2. If the only light-deflecting body to be taken into account is the Sun, the `iauAticq` function can be used instead.
3. The star-independent parameters can be obtained by calling one of the functions `iauApci[13]`, `iauApcg[13]`, `iauApco[13]` or `iauApcs[13]`.
4. The array *b* contains *n* entries, one for each body to be considered. If *n* = 0, no gravitational light deflection will be applied, not even for the Sun.
5. The array *b* should include an entry for the Sun as well as for any planet or other body to be taken into account. The entries should be in the order in which the light passes the body.
6. In the entry in the *b* array for body *i*, the mass parameter `b[i-1].bm` can, as required, be adjusted in order to allow for such effects as quadrupole field.
7. The deflection limiter parameter `b[i].dl` is  $\phi^2/2$ , where  $\phi$  is the angular separation (in radians) between star and body at which limiting is applied. As  $\phi$  shrinks below the chosen threshold, the deflection is artificially reduced, reaching zero for  $\phi = 0$ . Example values suitable for a terrestrial observer, together with masses, are as follows:

body i	b[i-1].bm	b[i-1].dl
Sun	1.0	6e-6
Jupiter	0.00095435	3e-9
Saturn	0.00028574	3e-10

8. For efficiency, validation of the contents of the  $b$  array is omitted. The supplied masses must be greater than zero, the position and velocity vectors must be right, and the deflection limiter greater than zero.

**iauAtio13***CIRS* → *observed***iauAtio13****CALL :**

```
status = iauAtio13 ( ri, di, utc1, utc2, dut1,
                    elong, phi, hm, xp, yp,
                    phpa, tc, rh, wl, aob, zob, hob, dob, rob );
```

**ACTION :**

CIRS  $[\alpha, \delta]$  to observed place. The caller supplies UTC, site coordinates, ambient air conditions and observing wavelength.

**GIVEN :**

<i>ri, di</i>	double	CIRS $[\alpha, \delta]$ (radians)
<i>utc1</i>	double	UTC as a 2-part...
<i>utc2</i>	double	... quasi Julian Date (Notes 1,2)
<i>dut1</i>	double	UT1–UTC (seconds, Note 3)
<i>elong</i>	double	longitude (radians, east-positive, Note 4)
<i>phi</i>	double	geodetic latitude (radians, Note 4)
<i>hm</i>	double	height above ellipsoid (m, geodetic Notes 4,6)
<i>xp, yp</i>	double	polar motion coordinates (radians, Note 5)
<i>phpa</i>	double	pressure at the observer (hPa $\equiv$ mB, Note 6)
<i>tc</i>	double	ambient temperature at the observer (deg C)
<i>rh</i>	double	relative humidity at the observer (range 0-1)
<i>wl</i>	double	wavelength (micrometers, Note 7)

**RETURNED :**

<i>aob</i>	double*	observed azimuth (radians: N=0°, E=90°)
<i>zob</i>	double*	observed zenith distance (radians)
<i>hob</i>	double*	observed hour angle (radians)
<i>dob</i>	double*	observed declination (radians)
<i>rob</i>	double*	observed right ascension (CIO-based, radians)
<i>eo</i>	double*	equation of the origins (ERA–GST)

**RETURNED** (function value) :

int	status:	+1 = dubious year (Note 2)
		0 = OK
		-1 = unacceptable date

## NOTES :

1.  $utc1+utc2$  is quasi Julian Date (see Note 2), apportioned in any convenient way between the two arguments, for example where  $utc1$  is the Julian Day Number and  $utc2$  is the fraction of a day. However, JD cannot unambiguously represent UTC during a leap second unless special measures are taken. The convention in the present function is that the JD day represents UTC days whether the length is 86399, 86400 or 86401 SI seconds.

Applications should use the function `iauDtF2d` to convert from calendar date and time of day into two-part quasi Julian Date, as it implements the leap-second-ambiguity convention just described.

2. The warning status “dubious year” flags UTCs that predate the introduction of the time scale or that are too far in the future to be trusted. See `iauDat` for further details.
3. UT1–UTC is tabulated in IERS bulletins. It increases by exactly one second at the end of each positive UTC leap second, introduced in order to keep UT1–UTC within  $\pm 0.9$ s. *n.b.* This practice is under review, and in the future UT1–UTC may grow essentially without limit.
4. The geographical coordinates are with respect to the WGS84 reference ellipsoid. **Take care with the longitude sign:** the longitude required by the present function is east-positive (*i.e.* right-handed), in accordance with geographical convention.
5. The polar motion  $xp, yp$  can be obtained from IERS bulletins. The values are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System (see IERS Conventions 2003), measured along the meridians  $0^\circ$  and  $90^\circ$  west respectively. For many applications,  $xp$  and  $yp$  can be set to zero.
6. If  $h$ , the height above the ellipsoid of the observing station in meters, is not known but  $p$ , the pressure in hPa ( $\equiv$ mB), is available, an adequate estimate of  $h$  can be obtained from the expression

$$h = -29.3 t_0 \log(p/1013.25)$$

where  $t_0$  is the approximate sea-level air temperature in K (See *Astrophysical Quantities*, C.W. Allen, 3rd edition, Section 52). Similarly, if the pressure  $p$  is not known, it can be estimated from the height of the observing station,  $h$ , as follows:

$$p = 1013.25 e^{-h/(29.3t_0)}$$

Note, however, that the refraction is nearly proportional to the pressure and that an accurate  $p$  value is important for precise work.

7. The argument  $wl$  specifies the observing wavelength in micrometers. The transition from optical to radio is assumed to occur at  $100 \mu\text{m}$  (about 3000 GHz).
8. “Observed” azimuth and zenith distance means the position that would be seen by a perfect geodetically aligned theodolite. (Zenith distance is used rather than altitude in order to reflect the fact that no allowance is made for depression of the horizon.)

This is related to the observed  $[h, \delta]$  *via* the standard rotation, using the geodetic latitude (corrected for polar motion), while the observed  $h$  and  $\alpha$  are related simply through the Earth rotation angle and the site longitude. “Observed”  $[\alpha, \delta]$  or  $[h, \delta]$  thus means the position that would be seen by a perfect equatorial with its polar axis aligned to the Earth’s axis of rotation.

9. The accuracy of the result is limited by the corrections for refraction, which use a simple  $A \tan \zeta + B \tan^3 \zeta$  model. Providing the meteorological parameters are known accurately and there are no gross local effects, the predicted observed coordinates should be within 0<sup>′</sup>.05 (optical) 1<sup>′</sup> (radio) for  $\zeta < 70^\circ$ , better than 30<sup>′</sup> (optical or radio) at  $85^\circ$  and better than 0<sup>′</sup>.3 (optical) or 0<sup>′</sup>.5 (radio) at the horizon.

Without refraction, the complementary functions `iauAtio13` and `iauAtoi13` are self-consistent to better than 1  $\mu$ as all over the celestial sphere. With refraction included, consistency falls off at high zenith distances, but is still better than 0<sup>′</sup>.05 at  $\zeta = 85^\circ$ .

10. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.

---

<b>iauAtioq</b>	<i>quick CIRS</i> → <i>observed</i>	<b>iauAtioq</b>
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---

**CALL :**

```
iauAtioq ( ri, di, &astrom, &aob, &zob, &hob, &dob, &rob );
```

**ACTION :**

Quick CIRS to observed place transformation.

**GIVEN :**

<i>ri, di</i>	double	CIRS [ $\alpha, \delta$ ] (radians)
<i>astrom</i>	iauASTROM*	star-independent astrometry parameters

**RETURNED :**

<i>aob</i>	double*	observed azimuth (radians: N=0°, E=90°)
<i>zob</i>	double*	observed zenith distance (radians)
<i>hob</i>	double*	observed hour angle (radians)
<i>dob</i>	double*	observed declination (radians)
<i>rob</i>	double*	observed right ascension (CIO-based, radians)

**NOTES :**

1. This function returns zenith distance rather than altitude in order to reflect the fact that no allowance is made for depression of the horizon.
2. The accuracy of the result is limited by the corrections for refraction, which use a simple  $A \tan \zeta + B \tan^3 \zeta$  model. Providing the meteorological parameters are known accurately and there are no gross local effects, the predicted observed coordinates should be within 0".05 (optical) 1" (radio) for  $\zeta < 70^\circ$ , better than 30" (optical or radio) at  $85^\circ$  and better than 0".3 (optical) or 0".5 (radio) at the horizon.

Without refraction, the complementary functions `iauAtioq` and `iauAtoiq` are self-consistent to better than  $1 \mu\text{as}$  all over the celestial sphere. With refraction included, consistency falls off at high zenith distances, but is still better than 0".05 at  $\zeta = 85^\circ$ .

3. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.
4. The CIRS [ $\alpha, \delta$ ] is obtained from a star catalog mean place by allowing for space motion, parallax, the Sun's gravitational lens effect, annual aberration and precession-nutation. For star positions in the ICRS, these effects can be applied by means of the `iauAtci13` (*etc.*) functions. Starting from classical "mean place" systems, additional transformations will be needed first.
5. "Observed" azimuth and zenith distance means the position that would be seen by a perfect geodetically aligned theodolite. (Zenith distance is used rather than altitude in order to reflect the fact that no allowance is made for depression of the horizon.) This is related to the observed [ $h, \delta$ ] *via* the standard rotation, using the geodetic latitude (corrected for polar motion), while the observed  $h$  and  $\alpha$  are related simply through the Earth rotation angle and the site longitude. "Observed" [ $\alpha, \delta$ ] or [ $h, \delta$ ] thus means the position that would be seen by a perfect equatorial with its polar axis aligned to the Earth's axis of rotation.

6. The star-independent astrometry parameters in *astrom* may be computed with `iauApio[13]` or `iauApc0[13]`. If nothing has changed significantly except the time, `iauAper[13]` may be used to perform the requisite adjustment to the *astrom* structure.

**iauAtoc13***observed* → *astrometric ICRS***iauAtoc13****CALL :**

```
status = iauAtoc13 ( type, ob1, ob2, utc1, utc2, dut1,
                   elong, phi, hm, xp, yp, phpa, tc, rh, wl, &rc, &dc );
```

**ACTION :**

Observed place at a groundbased site to ICRS astrometric  $[\alpha, \delta]$ . The caller supplies UTC, site coordinates, ambient air conditions and observing wavelength.

**GIVEN :**

<i>type</i>	char*	type of coordinates – R, H or A (Notes 1,2)
<i>ob1</i>	double	observed Az, HA or RA (radians; Az is N=0°, E=90°)
<i>ob2</i>	double	observed ZD or Dec (radians)
<i>utc1</i>	double	UTC as a 2-part...
<i>utc2</i>	double	... quasi Julian Date (Notes 3,4)
<i>dut1</i>	double	UT1–UTC (seconds, Note 5)
<i>elong</i>	double	longitude (radians, east-positive, Note 6)
<i>phi</i>	double	geodetic latitude (radians, Note 6)
<i>hm</i>	double	height above ellipsoid (m, geodetic Notes 6,8)
<i>xp,yp</i>	double	polar motion coordinates (radians, Note 7)
<i>phpa</i>	double	pressure at the observer (hPa ≡ mB, Note 8)
<i>tc</i>	double	ambient temperature at the observer (deg C)
<i>rh</i>	double	relative humidity at the observer (range 0-1)
<i>wl</i>	double	wavelength (micrometers, Note 9)

**RETURNED :**

<i>rc,dc</i>	double*	ICRS astrometric $[\alpha, \delta]$
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**RETURNED** (function value) :

int	status:	+1 = dubious year (Note 2)
		0 = OK
		-1 = unacceptable date

**NOTES :**

1. “Observed” azimuth and zenith distance means the position that would be seen by a perfect geodetically aligned theodolite. (Zenith distance is used rather than altitude in order to reflect the fact that no allowance is made for depression of the horizon.) This is related to the observed  $[h, \delta]$  *via* the standard rotation, using the geodetic latitude (corrected for polar motion), while the observed  $h$  and  $\alpha$  are related simply through the Earth rotation angle and the site longitude. “Observed”  $[\alpha, \delta]$  or  $[h, \delta]$  thus means the position that would be seen by a perfect equatorial with its polar axis aligned to the Earth’s axis of rotation.

2. Only the first character of the *type* argument is significant. “R” or “r” indicates that *ob1* and *ob2* are the observed right ascension and declination; “H” or “h” indicates that they are hour angle (west-positive) and declination; anything else (“A” or “a” is recommended) indicates that *ob1* and *ob2* are azimuth (north zero, east degi90) and zenith distance.
3. *utc1+utc2* is quasi Julian Date (see Note 4), apportioned in any convenient way between the two arguments, for example where *utc1* is the Julian Day Number and *utc2* is the fraction of a day. However, JD cannot unambiguously represent UTC during a leap second unless special measures are taken. The convention in the present function is that the JD day represents UTC days whether the length is 86399, 86400 or 86401 SI seconds.

Applications should use the function `iauDtF2d` to convert from calendar date and time of day into two-part quasi Julian Date, as it implements the leap-second-ambiguity convention just described.

4. The warning status “dubious year” flags UTCs that predate the introduction of the time scale or that are too far in the future to be trusted. See `iauDat` for further details.
5. UT1–UTC is tabulated in IERS bulletins. It increases by exactly one second at the end of each positive UTC leap second, introduced in order to keep UT1–UTC within  $\pm 0.9$ s. *n.b.* This practice is under review, and in the future UT1–UTC may grow essentially without limit.
6. The geographical coordinates are with respect to the WGS84 reference ellipsoid. **Take care with the longitude sign:** the longitude required by the present function is east-positive (*i.e.* right-handed), in accordance with geographical convention.
7. The polar motion *xp,yp* can be obtained from IERS bulletins. The values are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System (see IERS Conventions 2003), measured along the meridians  $0^\circ$  and  $90^\circ$  west respectively. For many applications, *xp* and *yp* can be set to zero.
8. If *h*, the height above the ellipsoid of the observing station in meters, is not known but *p*, the pressure in hPa ( $\equiv$ mB), is available, an adequate estimate of *h* can be obtained from the expression

$$h = -29.3 t_0 \log(p/1013.25)$$

where  $t_0$  is the approximate sea-level air temperature in K (See *Astrophysical Quantities*, C.W. Allen, 3rd edition, Section 52). Similarly, if the pressure *p* is not known, it can be estimated from the height of the observing station, *h*, as follows:

$$p = 1013.25 e^{-h/(29.3t_0)}$$

Note, however, that the refraction is nearly proportional to the pressure and that an accurate *p* value is important for precise work.

9. The argument *wl* specifies the observing wavelength in micrometers. The transition from optical to radio is assumed to occur at  $100 \mu\text{m}$  (about 3000 GHz).

10. The accuracy of the result is limited by the corrections for refraction, which use a simple  $A \tan \zeta + B \tan^3 \zeta$  model. Providing the meteorological parameters are known accurately and there are no gross local effects, the predicted observed coordinates should be within  $0''.05$  (optical)  $1''$  (radio) for  $\zeta < 70^\circ$ , better than  $30''$  (optical or radio) at  $85^\circ$  and better than  $0''.3$  (optical) or  $0''.5$  (radio) at the horizon.

Without refraction, the complementary functions `iauAtco13` and `iauAtoc13` are self-consistent to better than  $1 \mu\text{as}$  all over the celestial sphere. With refraction included, consistency falls off at high zenith distances, but is still better than  $0''.05$  at  $\zeta = 85^\circ$ .

11. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.

---

**iauAtoi13** *observed* → *CIRS* **iauAtoi13**


---

**CALL :**

```
status = iauAtoi13 ( type, ob1, ob2, utc1, utc2, dut1,
                  elong, phi, hm, xp, yp, phpa, tc, rh, wl, &ri, &di );
```

**ACTION :**

Observed place to CIRS. The caller supplies UTC, site coordinates, ambient air conditions and observing wavelength.

**GIVEN :**

<i>type</i>	char*	type of coordinates – R, H or A (Notes 1,2)
<i>ob1</i>	double	observed Az, HA or RA (radians; Az is N=0°, E=90°)
<i>ob2</i>	double	observed ZD or Dec (radians)
<i>utc1</i>	double	UTC as a 2-part...
<i>utc2</i>	double	... quasi Julian Date (Notes 3,4)
<i>dut1</i>	double	UT1–UTC (seconds, Note 5)
<i>elong</i>	double	longitude (radians, east-positive, Note 6)
<i>phi</i>	double	geodetic latitude (radians, Note 6)
<i>hm</i>	double	height above ellipsoid (m, geodetic Notes 6,8)
<i>xp,yp</i>	double	polar motion coordinates (radians, Note 7)
<i>phpa</i>	double	pressure at the observer (hPa ≡ mB, Note 8)
<i>tc</i>	double	ambient temperature at the observer (deg C)
<i>rh</i>	double	relative humidity at the observer (range 0-1)
<i>wl</i>	double	wavelength (micrometers, Note 9)

**RETURNED :**

<i>ri,di</i>	double*	CIRS [ $\alpha, \delta$ ]
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**RETURNED** (function value) :

<b>int</b>	status:	+1 = dubious year (Note 2)
		0 = OK
		-1 = unacceptable date

**NOTES :**

1. “Observed” azimuth and zenith distance means the position that would be seen by a perfect geodetically aligned theodolite. (Zenith distance is used rather than altitude in order to reflect the fact that no allowance is made for depression of the horizon.) This is related to the observed [ $h, \delta$ ] *via* the standard rotation, using the geodetic latitude (corrected for polar motion), while the observed  $h$  and  $\alpha$  are related simply through the Earth rotation angle and the site longitude. “Observed” [ $\alpha, \delta$ ] or [ $h, \delta$ ] thus means the position that would be seen by a perfect equatorial with its polar axis aligned to the Earth’s axis of rotation.

2. Only the first character of the *type* argument is significant. “R” or “r” indicates that *ob1* and *ob2* are the observed right ascension and declination; “H” or “h” indicates that they are hour angle (west-positive) and declination; anything else (“A” or “a” is recommended) indicates that *ob1* and *ob2* are azimuth (north zero, east degi90) and zenith distance.
3. *utc1+utc2* is quasi Julian Date (see Note 4), apportioned in any convenient way between the two arguments, for example where *utc1* is the Julian Day Number and *utc2* is the fraction of a day. However, JD cannot unambiguously represent UTC during a leap second unless special measures are taken. The convention in the present function is that the JD day represents UTC days whether the length is 86399, 86400 or 86401 SI seconds.

Applications should use the function `iauDtF2d` to convert from calendar date and time of day into two-part quasi Julian Date, as it implements the leap-second-ambiguity convention just described.

4. The warning status “dubious year” flags UTCs that predate the introduction of the time scale or that are too far in the future to be trusted. See `iauDat` for further details.
5. UT1–UTC is tabulated in IERS bulletins. It increases by exactly one second at the end of each positive UTC leap second, introduced in order to keep UT1–UTC within  $\pm 0.9$ s. *n.b.* This practice is under review, and in the future UT1–UTC may grow essentially without limit.
6. The geographical coordinates are with respect to the WGS84 reference ellipsoid. **Take care with the longitude sign:** the longitude required by the present function is east-positive (*i.e.* right-handed), in accordance with geographical convention.
7. The polar motion *xp,yp* can be obtained from IERS bulletins. The values are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System (see IERS Conventions 2003), measured along the meridians  $0^\circ$  and  $90^\circ$  west respectively. For many applications, *xp* and *yp* can be set to zero.
8. If *h*, the height above the ellipsoid of the observing station in meters, is not known but *p*, the pressure in hPa ( $\equiv$ mB), is available, an adequate estimate of *h* can be obtained from the expression

$$h = -29.3 t_0 \log(p/1013.25)$$

where  $t_0$  is the approximate sea-level air temperature in K (See *Astrophysical Quantities*, C.W. Allen, 3rd edition, Section 52). Similarly, if the pressure *p* is not known, it can be estimated from the height of the observing station, *h*, as follows:

$$p = 1013.25 e^{-h/(29.3t_0)}$$

Note, however, that the refraction is nearly proportional to the pressure and that an accurate *p* value is important for precise work.

9. The argument *wl* specifies the observing wavelength in micrometers. The transition from optical to radio is assumed to occur at  $100 \mu\text{m}$  (about 3000 GHz).

10. The accuracy of the result is limited by the corrections for refraction, which use a simple  $A \tan \zeta + B \tan^3 \zeta$  model. Providing the meteorological parameters are known accurately and there are no gross local effects, the predicted observed coordinates should be within 0".05 (optical) 1" (radio) for  $\zeta < 70^\circ$ , better than 30" (optical or radio) at  $85^\circ$  and better than 0.3 (optical) or 0.5 (radio) at the horizon.

Without refraction, the complementary functions `iauAtio13` and `iauAtoi13` are self-consistent to better than 1  $\mu$ as all over the celestial sphere. With refraction included, consistency falls off at high zenith distances, but is still better than 0".05 at  $\zeta = 85^\circ$ .

11. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.

---

<b>iauAtoiq</b>	<i>quick observed</i> → CIRS	<b>iauAtoiq</b>
-----------------	------------------------------	-----------------

---

**CALL :**

```
iauAtoiq ( type, ob1, ob2, &astrom, &ri, &di );
```

**ACTION :**

Quick observed place to CIRS transformation, given the star-independent astrometry parameters.

**GIVEN :**

<i>type</i>	<b>char*</b>	type of coordinates – R, H or A (Notes 1,2)
<i>ob1</i>	<b>double</b>	observed Az, HA or RA (radians; Az is N=0°, E=90°)
<i>ob2</i>	<b>double</b>	observed ZD or Dec (radians)
<i>astrom</i>	<b>iauASTROM*</b>	star-independent astrometry parameters

**RETURNED :**

<i>ri, di</i>	<b>double*</b>	CIRS [ $\alpha, \delta$ ]
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**NOTES :**

1. Only the first character of the *type* argument is significant. “R” or “r” indicates that *ob1* and *ob2* are the observed right ascension and declination; “H” or “h” indicates that they are hour angle (west-positive) and declination; anything else (“A” or “a” is recommended) indicates that *ob1* and *ob2* are azimuth (north zero, east degi90) and zenith distance.
2. “Observed” azimuth and zenith distance means the position that would be seen by a perfect geodetically aligned theodolite. (Zenith distance is used rather than altitude in order to reflect the fact that no allowance is made for depression of the horizon.) This is related to the observed [ $h, \delta$ ] via the standard rotation, using the geodetic latitude (corrected for polar motion), while the observed  $h$  and  $\alpha$  are related simply through the Earth rotation angle and the site longitude. “Observed” [ $\alpha, \delta$ ] or [ $h, \delta$ ] thus means the position that would be seen by a perfect equatorial with its polar axis aligned to the Earth’s axis of rotation.
3. The accuracy of the result is limited by the corrections for refraction, which use a simple  $A \tan \zeta + B \tan^3 \zeta$  model. Providing the meteorological parameters are known accurately and there are no gross local effects, the predicted observed coordinates should be within 0".05 (optical) 1" (radio) for  $\zeta < 70^\circ$ , better than 30" (optical or radio) at  $85^\circ$  and better than 0".3 (optical) or 0".5 (radio) at the horizon.  
 Without refraction, the complementary functions *iauAtioq* and *iauAtoiq* are self-consistent to better than 1  $\mu$ as all over the celestial sphere. With refraction included, consistency falls off at high zenith distances, but is still better than 0".05 at  $\zeta = 85^\circ$ .
4. It is advisable to take great care with units, as even unlikely values of the input parameters are accepted and processed in accordance with the models used.
5. The star-independent astrometry parameters in *astrom* may be computed with *iauApio*[13] or *iauApc0*[13]. If nothing has changed significantly except the time, *iauAper*[13] may be used to perform the requisite adjustment to the *astrom* structure.

---

**iauLd** *light deflection by a solar-system body* **iauLd**

**CALL :**

```
iauLd ( bm, p, q, e, em, dlim, p1 );
```

**ACTION :**

Apply light deflection by a solar-system body, as part of transforming coordinate direction into natural direction.

**GIVEN :**

<i>bm</i>	double	mass of the gravitating body (solar masses)
<i>p</i>	double[3]	direction from observer to source (unit vector)
<i>q</i>	double[3]	direction from body to source (unit vector)
<i>e</i>	double[3]	direction from body to observer (unit vector)
<i>em</i>	double	distance from body to observer (au)
<i>dlim</i>	double	deflection limiter (Note 4)

**RETURNED :**

<i>p1</i>	double[3]	observer to deflected source (unit vector)
-----------	-----------	--

**NOTES :**

1. The algorithm is based on Eq. (70) in Klioner (2003) and Eq. (7.63) in Urban & Seidelmann (2013), with some rearrangement to minimize the effects of machine precision.
2. The mass parameter *bm* can, as required, be adjusted in order to allow for such effects as quadrupole field.
3. The barycentric position of the deflecting body should ideally correspond to the time of closest approach of the light ray to the body.
4. The deflection limiter parameter *dlim* is  $\phi^2/2$ , where  $\phi$  is the separation (in radians) between star and body at which limiting is applied. As  $\phi$  shrinks below the chosen threshold, the deflection is artificially reduced, reaching zero for  $\phi = 0$ .
5. The returned vector *p1* is not normalized, but the consequential departure from unit magnitude is always negligible.
6. The arguments *p* and *p1* can be the same array.
7. To accumulate total light deflection taking into account the contributions from several bodies, call the present routine for each body in succession, in decreasing order of distance from the observer.
8. For efficiency, validation is omitted. The supplied vectors must be of unit magnitude, and the deflection limiter non-zero and positive.

---

**iauLdn** *light deflection by  $n$  solar-system bodies* **iauLdn**


---

**CALL :**

```
iauLdn ( n, b, ob, sc, sn );
```

**ACTION :**

For a star, apply light deflection by multiple solar-system bodies, as part of transforming coordinate direction into natural direction.

**GIVEN :**

<i>n</i>	<b>int</b>	number of bodies (Note 1)
<i>b</i>	<b>iauLDBODY[n]</b>	data for each of the $n$ bodies (Notes 1,2)
<i>ob</i>	<b>double[3]</b>	barycentric position of the observer (au)
<i>sc</i>	<b>double[3]</b>	observer to star coordinate direction (unit vector)

**RETURNED :**

<i>sn</i>	<b>double[3]</b>	observer to deflected star (unit vector)
-----------	------------------	--

**NOTES :**

1. The array *b* contains  $n$  entries, one for each body to be considered. If  $n = 0$ , no gravitational light deflection will be applied, not even for the Sun.
2. The array *b* should include an entry for the Sun as well as for any planet or other body to be taken into account. The entries should be in the order in which the light passes the body.
3. In the entry in the *b* array for body *i*, the mass parameter **b[i-1].bm** can, as required, be adjusted in order to allow for such effects as quadrupole field.
4. The deflection limiter parameter **b[i].dl** is  $\phi^2/2$ , where  $\phi$  is the angular separation (in radians) between star and body at which limiting is applied. As  $\phi$  shrinks below the chosen threshold, the deflection is artificially reduced, reaching zero for  $\phi = 0$ . Example values suitable for a terrestrial observer, together with masses, are as follows:

body <i>i</i>	<b>b[i-1].bm</b>	<b>b[i-1].dl</b>
Sun	1.0	6e-6
Jupiter	0.00095435	3e-9
Saturn	0.00028574	3e-10

5. For cases where the starlight passes the body before reaching the observer, the body is placed back along its barycentric track by the light time from that point to the observer. For cases where the body is “behind” the observer no such shift is applied. If a different treatment is preferred, the user has the option of instead using the **iauLd** function. Similarly, **iauLd** can be used for cases where the source is nearby, not a star.
6. The returned vector *sn* is not normalized, but the consequential departure from unit magnitude is always negligible.
7. For efficiency, validation is omitted. The supplied masses must be greater than zero, the position and velocity vectors must be right, and the deflection limiter greater than zero.

---

**iauLdsun** *light deflection by the Sun* **iauLdsun**

**CALL :**

```
iauLdsun ( p, e, em, p1 );
```

**ACTION :**

Light deflection by the Sun.

**GIVEN :**

<i>p</i>	double[3]	direction from observer to source (unit vector)
<i>e</i>	double[3]	direction from body to observer (unit vector)
<i>em</i>	double	distance from body to observer (au)

**RETURNED :**

<i>p1</i>	double[3]	observer to deflected source (unit vector)
-----------	-----------	--

**NOTES :**

1. The source is presumed to be sufficiently distant that its directions seen from the Sun and the observer are essentially the same.
2. The deflection is restrained when the angle between the star and the Sun's center is less than about 9", falling to zero for zero separation. (The chosen threshold is within the solar limb for all solar-system applications.)
3. The arguments *p* and *p1* can be the same array.

---

**iauPmpx***proper motion & parallax***iauPmpx****CALL :**

```
iauPmpx ( rc, dc, pr, pd, px, rv, pmt, pob, pco );
```

**ACTION :**

Proper motion and parallax.

**GIVEN :**

<i>rc,dc</i>	double	ICRS [ $\alpha, \delta$ ] at catalog epoch (radians)
<i>pr</i>	double	RA proper motion (radians/year; Note 1)
<i>pd</i>	double	Dec proper motion (radians/year)
<i>px</i>	double	parallax (arcsec)
<i>rv</i>	double	radial velocity (km/s, positive if receding)
<i>pmt</i>	double	proper motion time interval (SSB, Julian years)
<i>pob</i>	double[3]	SSB to observer vector (au)

**RETURNED :**

<i>pco</i>	double[3]	coordinate direction (BCRS unit vector)
------------	-----------	---

**NOTES :**

1. The proper motion in right ascension is  $\dot{\alpha}$  rather than  $\dot{\alpha} \cos \delta$ .
2. To avoid the need for iteration, the Rømer effect (*i.e.* the small annual modulation of the proper motion coming from the changing light time) is applied approximately, using the direction of the star at the catalog epoch.
3. The algorithm used is non-relativistic: see the 1984 *Astronomical Almanac*, pp B39-B41, and Chapter 3 in Urban & Seidelmann (2013). An alternative implementation that uses an SR-compliant algorithm is given in Appendix A.

---

**iauPvtob** *observatory position and velocity* **iauPvtob**


---

**CALL :**

```
iauPvtob ( elong, phi, hm, xp, yp, sp, theta, pv );
```

**ACTION :**

Position and velocity of a terrestrial observing station.

**GIVEN :**

<i>elong</i>	double	longitude (radians, east-positive, Note 1)
<i>phi</i>	double	latitude (geodetic, radians, Note 1)
<i>hm</i>	double	height above reference ellipsoid (geodetic, m)
<i>xp,yp</i>	double	coordinates of the pole (radians, Note 2)
<i>sp</i>	double	the TIO locator $s'$ (radians, Note 2)
<i>theta</i>	double	Earth rotation angle (radians, Note 3)

**RETURNED :**

<i>pv</i>	double[2][3]	position/velocity vector (m, m/s, CIRS)
-----------	--------------	---

**NOTES :**

1. The terrestrial coordinates are with respect to the WGS84 reference ellipsoid.
2. *xp,yp* are the coordinates (in radians) of the Celestial Intermediate Pole with respect to the International Terrestrial Reference System, measured along the meridians  $0^\circ$  and  $\text{degi90}$  west respectively; see McCarthy & Petit (2003), Chapter 5. *sp* is the TIO locator  $s'$ , in radians, which positions the Terrestrial Intermediate Origin on the equator. For many applications, *xp*, *yp* and (especially) *sp* can be set to zero.
3. If *theta* is Greenwich apparent sidereal time instead of Earth rotation angle, the result is with respect to the true equator and equinox of date, *i.e.* with the *x*-axis at the equinox rather than the celestial intermediate origin.
4. The velocity units are meters per UT1 second, not per SI second. This is unlikely to have any practical consequences in the modern era.
5. No validation is performed on the arguments. Error cases that could lead to arithmetic exceptions are trapped by the `iauGd2gc` function, and the result set to zeros.
6. See Section 7.4.3.3 in the *Explanatory Supplement*, 3rd edition, Urban & Seidelmann (2013).

---

**iauRefco***refraction constants***iauRefco****CALL :**

```
iauRefco ( phpa, tc, rh, wl, refa, refb );
```

**ACTION :**

Determine the constants  $A$  and  $B$  in the atmospheric refraction model

$$\Delta\zeta = A \tan \zeta + B \tan^3 \zeta.$$

$\zeta$  is the “observed” zenith distance (*i.e.* affected by refraction) and  $\Delta\zeta$  is what to add to give the “topocentric” (*i.e. in vacuo*) zenith distance.

**GIVEN :**

<i>phpa</i>	double	pressure at the observer (hPa $\equiv$ millibar)
<i>tc</i>	double	ambient temperature at the observer (degrees Celsius)
<i>rh</i>	double	relative humidity at the observer (1.0 means 100%)
<i>wl</i>	double	wavelength (micrometers)

**RETURNED :**

<i>refa</i>	double*	$\tan \zeta$ coefficient (radians)
<i>refb</i>	double*	$\tan^3 \zeta$ coefficient (radians)

**NOTES :**

1. The model balances speed and accuracy to give good results in applications where performance at low altitudes is not paramount. Performance is maintained across a range of conditions, and applies to both optical/IR and radio.
2. The influences of the following are neglected:
  - height above sea level, apart from the reduced pressure itself;
  - latitude, *i.e.* the flattening of the Earth;
  - variations in tropospheric lapse rate and height of tropopause;
  - dispersive effects in the radio.
3. The model was tested using the following range of conditions:
  - lapse rates 0.0055, 0.0065, 0.0075 K per meter
  - latitudes  $0^\circ$ ,  $25^\circ$ ,  $50^\circ$ ,  $75^\circ$
  - heights 0, 2500, 5000 meters above sea level
  - pressures, mean for height  $-10\%$  to  $+5\%$  in steps of 5%
  - temperatures  $-10^\circ$  to  $+20^\circ$  with respect to 280K at sea level
  - relative humidity 0, 0.5, 1
  - wavelength 0.4, 0.6, ...  $2\mu\text{m}$ , and radio

- zenith distances 15°, 45°, 75°

4. The accuracy with respect to raytracing through a model atmosphere was found to be as follows:

	<i>worst</i>	<i>RMS</i>
optical/IR	62	8
radio	319	49
	mas	mas

For this particular set of conditions:

- lapse rate 6.5 K km<sup>-1</sup>
- latitude 50°
- sea level
- pressure 1005 mb
- temperature 7°C
- humidity 80%
- wavelength 5740 Å

the results were as follows:

$\zeta$	raytrace	iauRefco	Saastamoinen
10	10.27	10.27	10.27
20	21.19	21.20	21.19
30	33.61	33.61	33.60
40	48.82	48.83	48.81
45	58.16	58.18	58.16
50	69.28	69.30	69.27
55	82.97	82.99	82.95
60	100.51	100.54	100.50
65	124.23	124.26	124.20
70	158.63	158.68	158.61
72	177.32	177.37	177.31
74	200.35	200.38	200.32
76	229.45	229.43	229.42
78	267.44	267.29	267.41
80	319.13	318.55	319.10
deg	arcsec	arcsec	arcsec

The values for Saastamoinen's formula (which includes terms up to  $\tan^5$ ) are taken from Hohenkerk & Sinclair (1985).

5. A *wl* value in the range 0-100 selects the optical/IR case and is wavelength in  $\mu\text{m}$ . Any value outside this range selects the radio case. Radio dispersion effects, important above 100 GHz, are neglected.
6. Outlandish input parameters are silently limited to mathematically safe values. Zero pressure is permissible, and causes zeroes to be returned.

- The formula for the saturation vapour pressure of water as a function of temperature and temperature is taken from Equations (A4.5-A4.7) of Gill (1982).
  - The formula for the water vapour pressure, given the saturation pressure and the relative humidity is from Crane (1976), Equation (2.5.5).
  - The refractivity of air is a function of temperature, total pressure, water-vapour pressure and, in the case of optical/IR, wavelength. The formulae for the two cases are developed from Hohenkerk & Sinclair (1985) and Rueger (2002).
  - The formula for  $\beta$  ( $= H_0/r_0$ ) is an adaption of Equation (9) from Stone (1996). The adaptations, arrived at empirically, consist of (i) a small adjustment to the coefficient and (ii) a humidity term for the radio case only.
  - The formulae for the refraction constants as a function of  $n - 1$  and  $\beta$  are from Green (1987), Equation (4.31).
7. The sign conventions for the coefficients are such that  $A$  is positive and  $B$  (much smaller) is negative.

## 8 Abbreviations

BCRS	Barycentric Celestial Reference System
CIO	Celestial Intermediate Origin
CIP	Celestial Intermediate Pole
CIRS	Celestial Intermediate Reference System
EO	equation of the origins
FK5	fifth fundamental catalog
GCRS	Geocentric Celestial Reference System
GR	general relativity
GST	Greenwich (apparent) sidereal time
IAU	International Astronomical Union
ICRS	International Celestial Reference System
IERS	International Earth Rotation and reference systems Service
ITRS	International Terrestrial Reference System
JD	Julian date
J2000.0	2000 January 1.5 (in some specified time scale)
MJD	Modified Julian date
SR	special relativity
SOFA	Standards of Fundamental Astronomy
TIO	Terrestrial Intermediate Origin
TIRS	Terrestrial Intermediate Reference System
TAI	International Atomic Time
TDB	Barycentric Dynamical Time
TT	Terrestrial Time
UT1	Universal Time
UTC	Coordinated Universal Time

## 9 References

- Allen, C.W., (1976). *Astrophysical Quantities*, University of London, The Athlone Press, 3rd ed.
- Crane, R.K., Meeks, M.L. (eds) (1976). *Refraction Effects in the Neutral Atmosphere*, Methods of Experimental Physics: Astrophysics 12B, Academic Press.
- Gill, Adrian E. (1982). *Atmosphere-Ocean Dynamics*, Academic Press.
- Green, R.M. (1987). *Spherical Astronomy*, Cambridge University Press.
- Hohenkerk, C.Y., & Sinclair, A.T. (1985). NAO Technical Note No. 63.
- Klioner, Sergei A. (2003). *A practical relativistic model for microarcsecond astrometry in space*, Astr. J. **125**, 1580-1597.
- McCarthy, D. D., Petit, G. (eds.) (2004). *IERS Conventions (2003)*, IERS Technical Note No. 32, Bundesamt für Kartographie und Geodäsie.
- Rueger, J.M. (2002). *Refractive Index Formulae for Electronic Distance Measurement with Radio and Millimetre Waves*, in Unisurv Report S-68, School of Surveying and Spatial Information Systems, University of New South Wales, Sydney, Australia.
- Stone, Ronald C. (1996). P.A.S.P. **108**, 1051-1058.
- Urban, Sean, & Seidelmann, P. Kenneth (eds.) (2013). *Explanatory Supplement to the Astronomical Almanac*, 3rd ed., University Science Books.

## Appendix: a relativistic version of the iauPmpx function

The standard SOFA proper motion and parallax function uses a robust non-relativistic formulation that meets all practical accuracy requirements. Here is an unreleased counterpart that is compliant with special relativity but relies upon the proper motion and parallax data being physically possible:

---

```

#include "sofa.h"

void iauPmpx(double rc, double dc, double pr, double pd,
             double px, double rv, double pmt, double pob[3],
             double pco[3])
/*
**  - - - - -
**   i a u P m p x
**  - - - - -
**
** Proper motion and parallax.
**
** Status:  unreleased SOFA support function.
**
** Given:
**   rc,dc  double      ICRS RA,Dec at catalog epoch (radians)
**   pr     double      RA proper motion (radians/year; Note 1)
**   pd     double      Dec proper motion (radians/year)
**   px     double      parallax (arcsec)
**   rv     double      radial velocity (km/s, +ve if receding)
**   pmt    double      proper motion time interval (SSB, Julian years)
**   vob    double[3]   SSB to observer vector (au)
**
** Returned:
**   pco    double[3]   coordinate direction (BCRS unit vector)
**
** Notes:
**
** 1) The proper motion in RA is dRA/dt rather than cos(Dec)*dRA/dt.
**
** 2) The proper motion time interval is for when the starlight
**    reaches the solar system barycenter.
**
** 3) To avoid the need for iteration, the Roemer effect (i.e. the
**    small annual modulation of the proper motion coming from the
**    changing light time) is applied approximately, using the
**    direction of the star at the catalog epoch.
**
** Called:

```

```

**      iauPdp      scalar product of two p-vectors
**      iauPmsafe   proper motion with small-parallax handling
**      iauS2c      spherical coordinates to unit vector
**      iauPn       decompose p-vector into modulus and direction
**
** Usual SOFA copyright terms apply.
*/
{
/* Light time for 1 au, days */
#define AULTD (AULT/DAYSEC)

    int j, i;
    double p[3], dt, rc2, dc2, pr2, pd2, px2, rv2, w;

/*-----*/

/* Barycentric direction of star at catalog epoch. */
    iauS2c(rc, dc, p);

/* Proper motion time interval (d), including Roemer effect. */
    dt = pmt*DJY + iauPdp(p,pob)*AULTD;

/* Space motion. */
    j = iauPmsafe(rc, dc, pr, pd, px, rv, DJMO, 0.0, DJMO, dt,
                 &rc2, &dc2, &pr2, &pd2, &px2, &rv2);

/* Barycentric direction of star at date. */
    iauS2c(rc2, dc2, p);

/* Parallax. */
    w = px2 * DAS2R;
    for ( i = 0; i < 3; i++ ) {
        p[i] -= w * pob[i];
    }
    iauPn(p, &w, pco);
}

```

---